

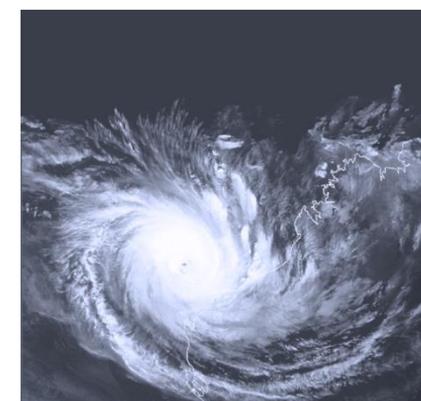


# Evolution of Soliton Measurement and Modelling

Presented by:  
Steve Buchan  
Kenji Shimizu

'With some deference  
to Garvey'

RPS MetOcean



# 14<sup>th</sup> IWWHF – Soliton Measurements & Modelling

For those who came in late ..... the previous presentation:

- Demonstrated the engineering need for soliton criteria
- Illustrated the plethora of soliton ‘types’ at North Rankin location
- Noted that measurements alone are insufficient
  - Can’t detail spatial structure
  - Can’t provide ‘enough’ events for reliable extreme analysis
  - Can’t extrapolate to adjacent sites
- Hence the need for nonhydrostatic modelling
- Trialled MITgcm – provides the mechanism, but not (yet) with accuracy.

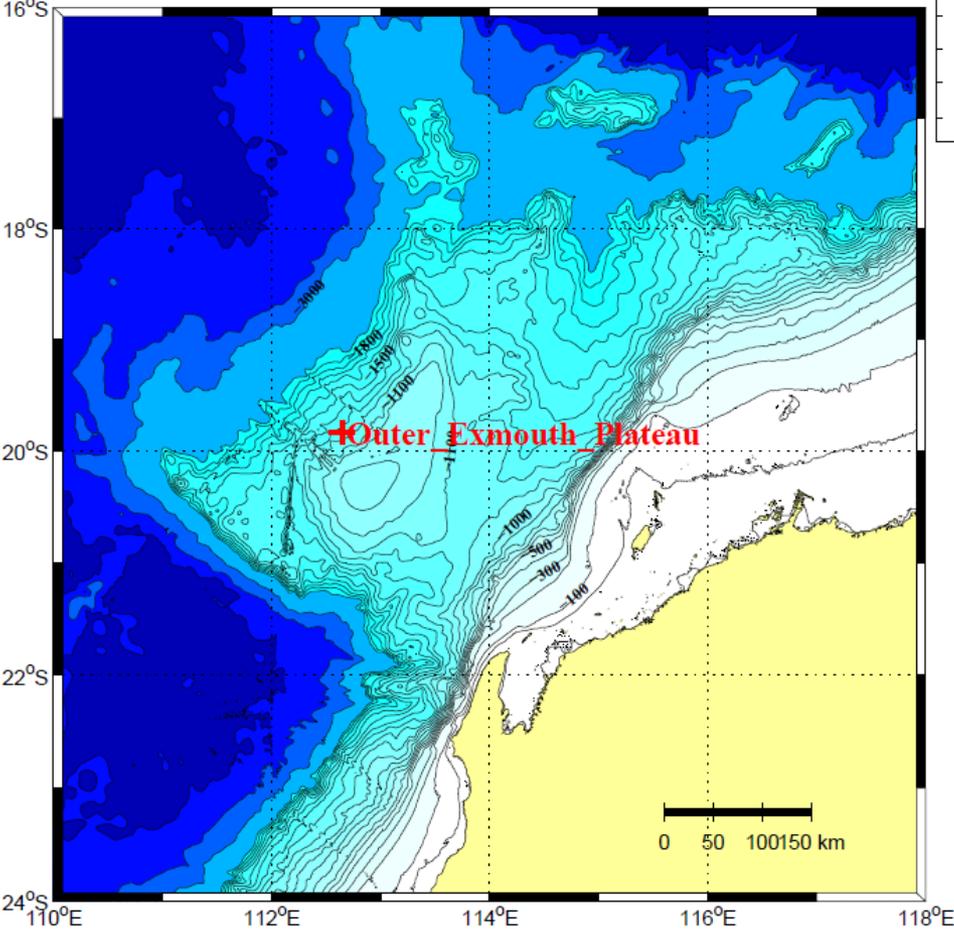
# Presentation Structure

- Discussion of recent measurements on Outer Exmouth Plateau
- Recognition of Indonesian Archipelago as potential source for (Australian) North West Shelf internal waves
- Reconfiguration of the NWS MITgcm modelling domain to include these possible source regions
- Resulting improvements to internal solitary wave simulation
- Qualitative comparisons to North Rankin and Shelf Break measurements

# Outer Exmouth Plateau Measurements

- 12 month Metocean Measurement programme to support planning for deepwater drilling operations (for Shell Australia)
- Measurements comprised
  - Meteorological (RPS buoy) measurements
  - Directional (Datawell Waverider) buoy measurements
  - Through-Water-Column current, temperature and salinity measurements
- In 1250 m of water
- The programme returned almost 100% good data.

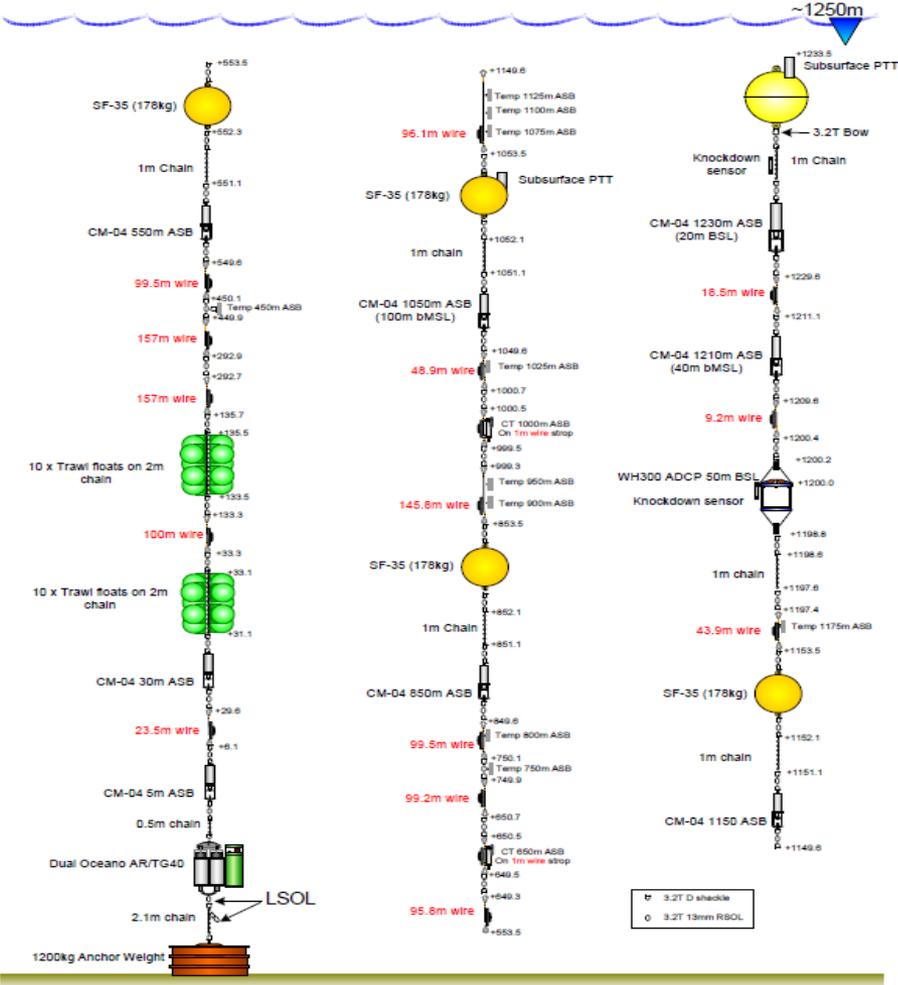
# Measurement Region



- WA-489-P
- 12 Months of
  - Met
  - Wave
  - TWC: Current
  - SWT

# Current Meter Mooring

## Outer Exmouth Plateau - Currents



## Instruments comprised:

- 8 x CM04s
- 1 x 300 kHz ADCP
- 10 x temp loggers
- 2 x CT loggers
- 1 x tide gauge

in 1250 m of water.

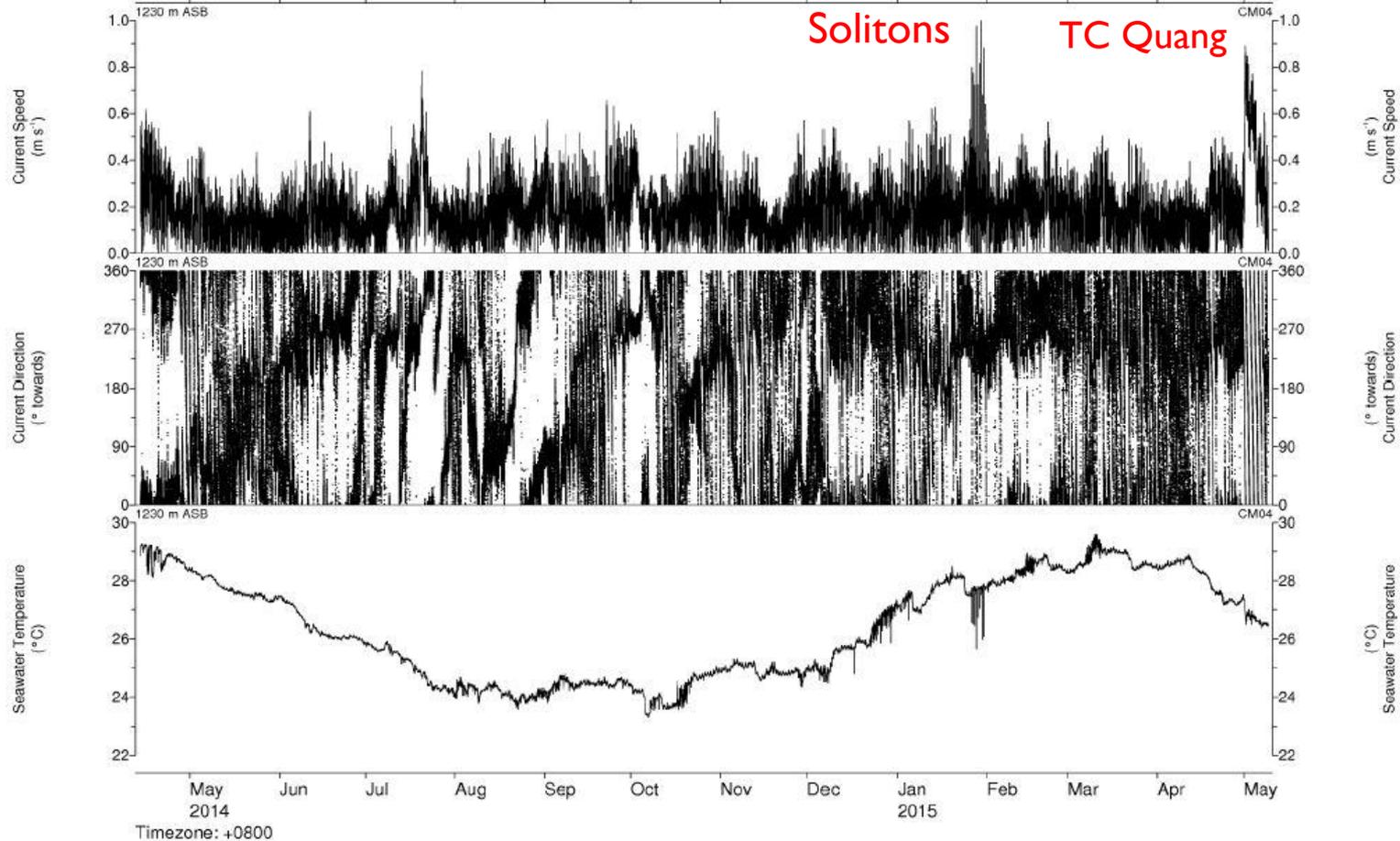
# Two Events of Major Note

1. (Almost) direct hit by Tropical Cyclone Quang
2. Extraordinary week of internal solitary wave activity.



# Outer Exmouth Surface Currents

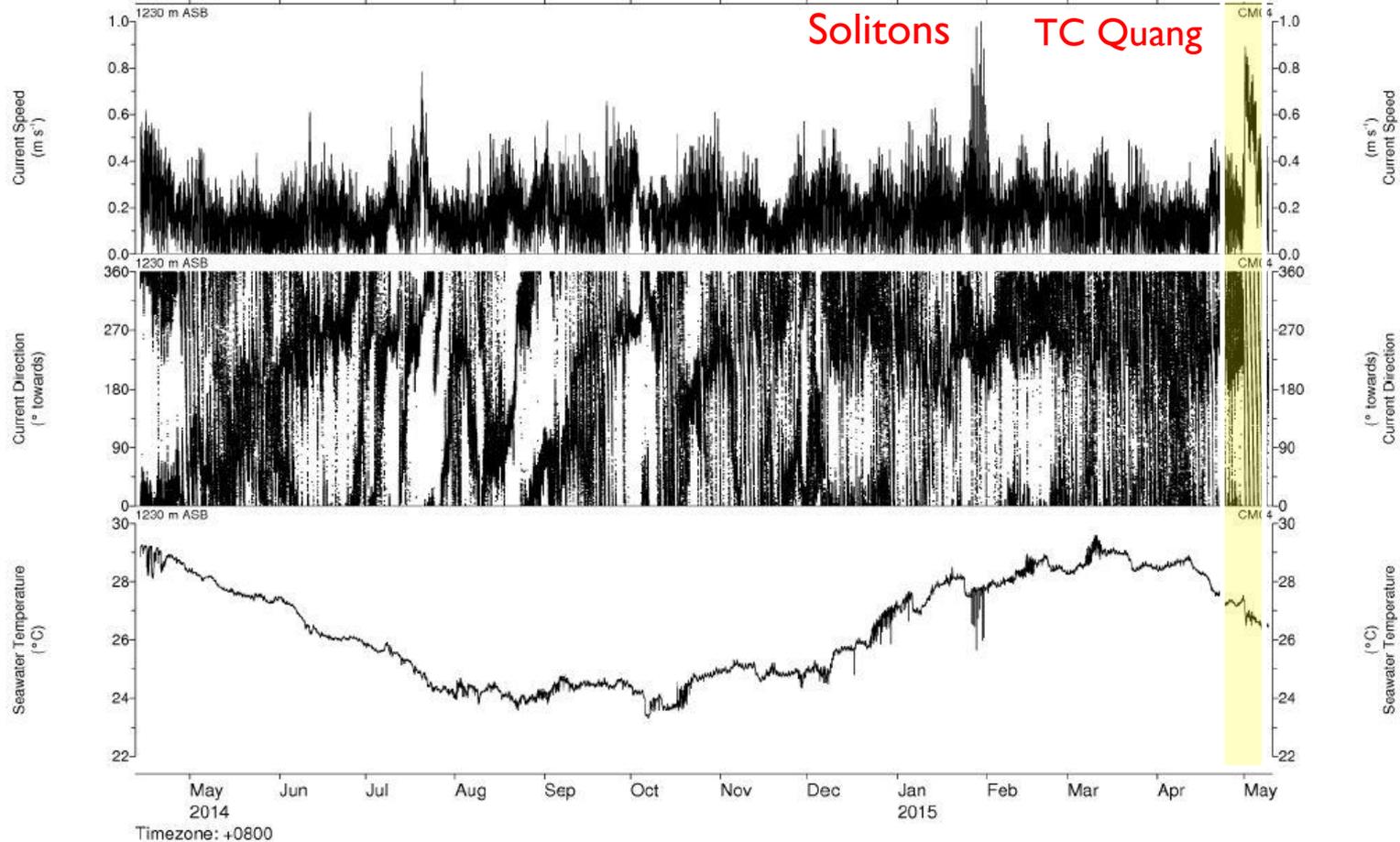
<b>Location:</b>	<b>Outer Exmouth Plateau</b>	<b>Client:</b>	Shell Development (Australia) Pty Ltd
Latitude:	19° 50' 4" S	Project:	J3003
Longitude:	112° 38' 38" E		
Location Water Depth:	1250.00 m MSL		





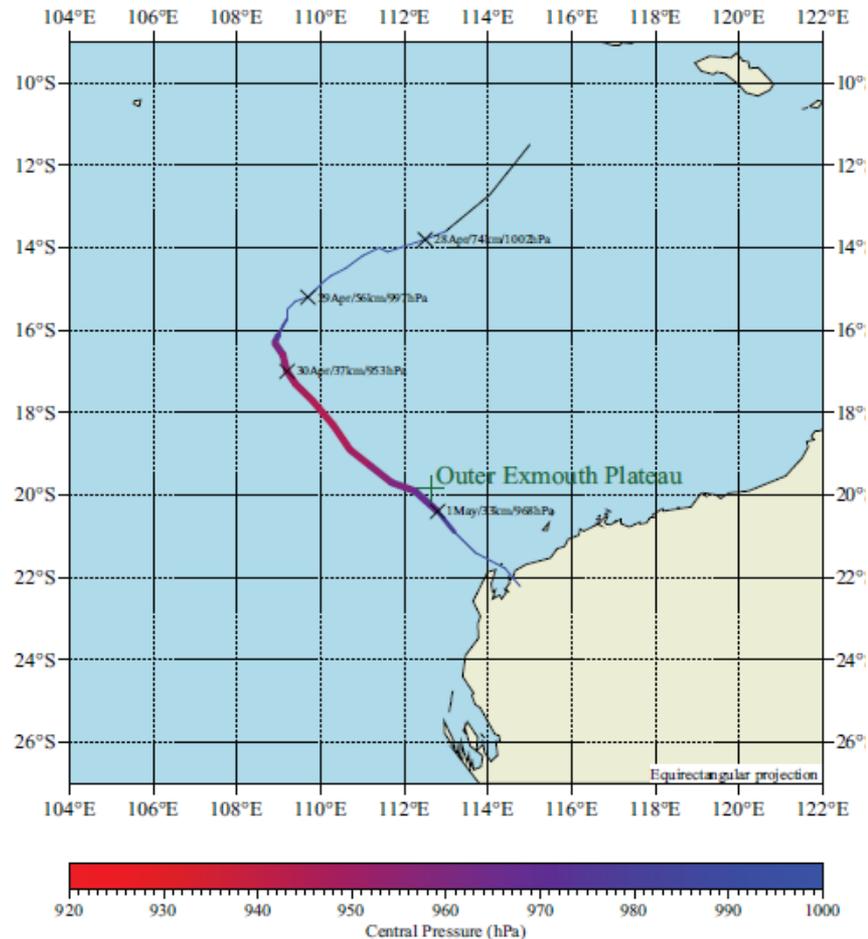
# Exmouth Surface Currents – TC Quang

<b>Location:</b>	<b>Outer Exmouth Plateau</b>	<b>Client:</b>	Shell Development (Australia) Pty Ltd
Latitude:	19° 50' 4" S	<b>Project:</b>	J3003
Longitude:	112° 38' 38" E		
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# Tropical Cyclone Quang

TC Quang



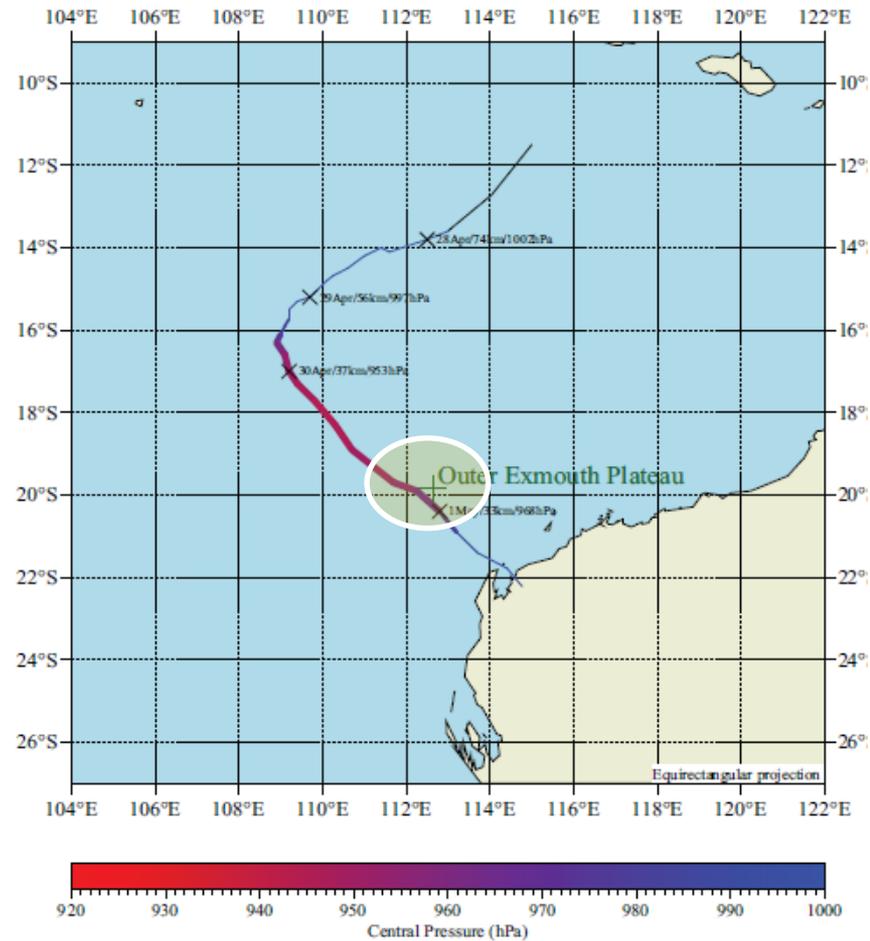
Legend	Central Pressure
—	missing
█	920 hPa
█	940 hPa
█	960 hPa
█	980 hPa
█	1000 hPa

Timestamps at midnight UTC  
 - Date  
 - Radius to Maximum Winds (km)  
 - Central Pressure (hPa)

27 April to 1 May 2015

# Tropical Cyclone Quang

TC Quang



Legend	Central Pressure
—	missing
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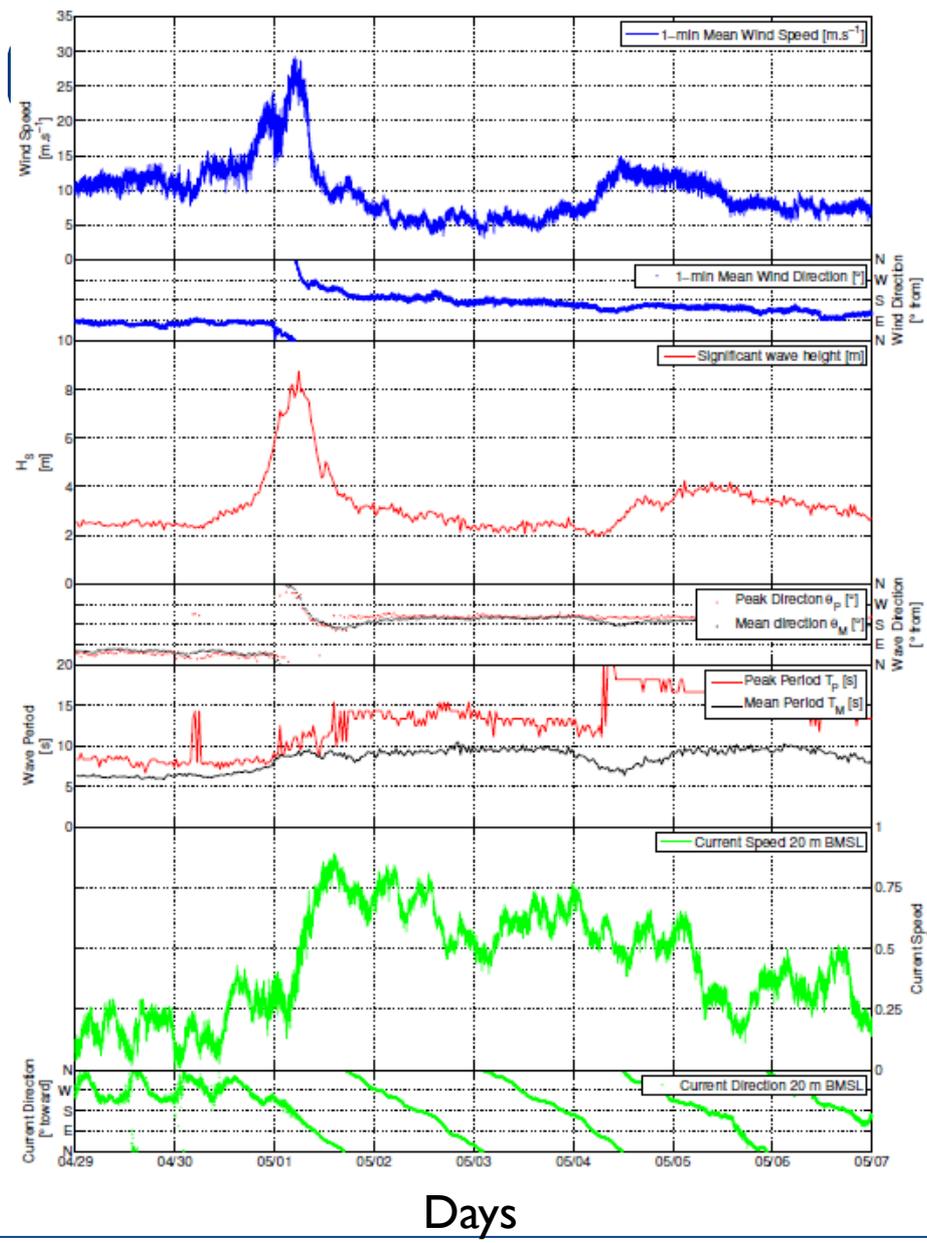
Timestamps at midnight UTC  
 - Date  
 - Radius to Maximum Winds (km)  
 - Central Pressure (hPa)

27 April to 1 May 2015

Peak Wind Speed  $U_{10} = 28 \text{ m s}^{-1}$

Peak Wave Height  $H_s = 8.7 \text{ m}$

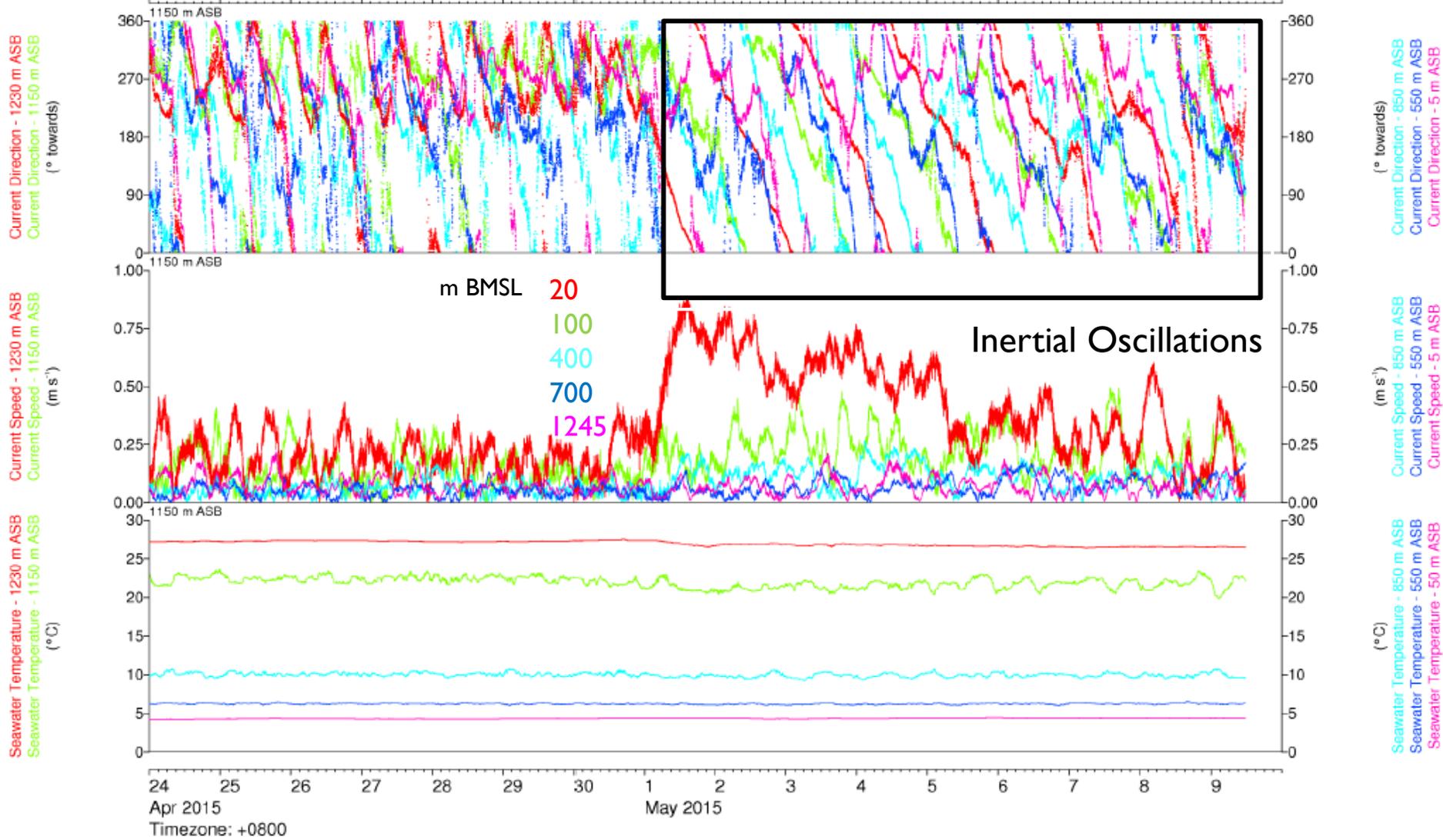
Peak Current Speed  $V_s = 0.9 \text{ m s}^{-1}$



**Location: Outer Exmouth Plateau - Currents**

Latitude: 19° 50' 7" S  
Longitude: 112° 38' 42" E  
Location Water Depth: 1250.00 m MSL

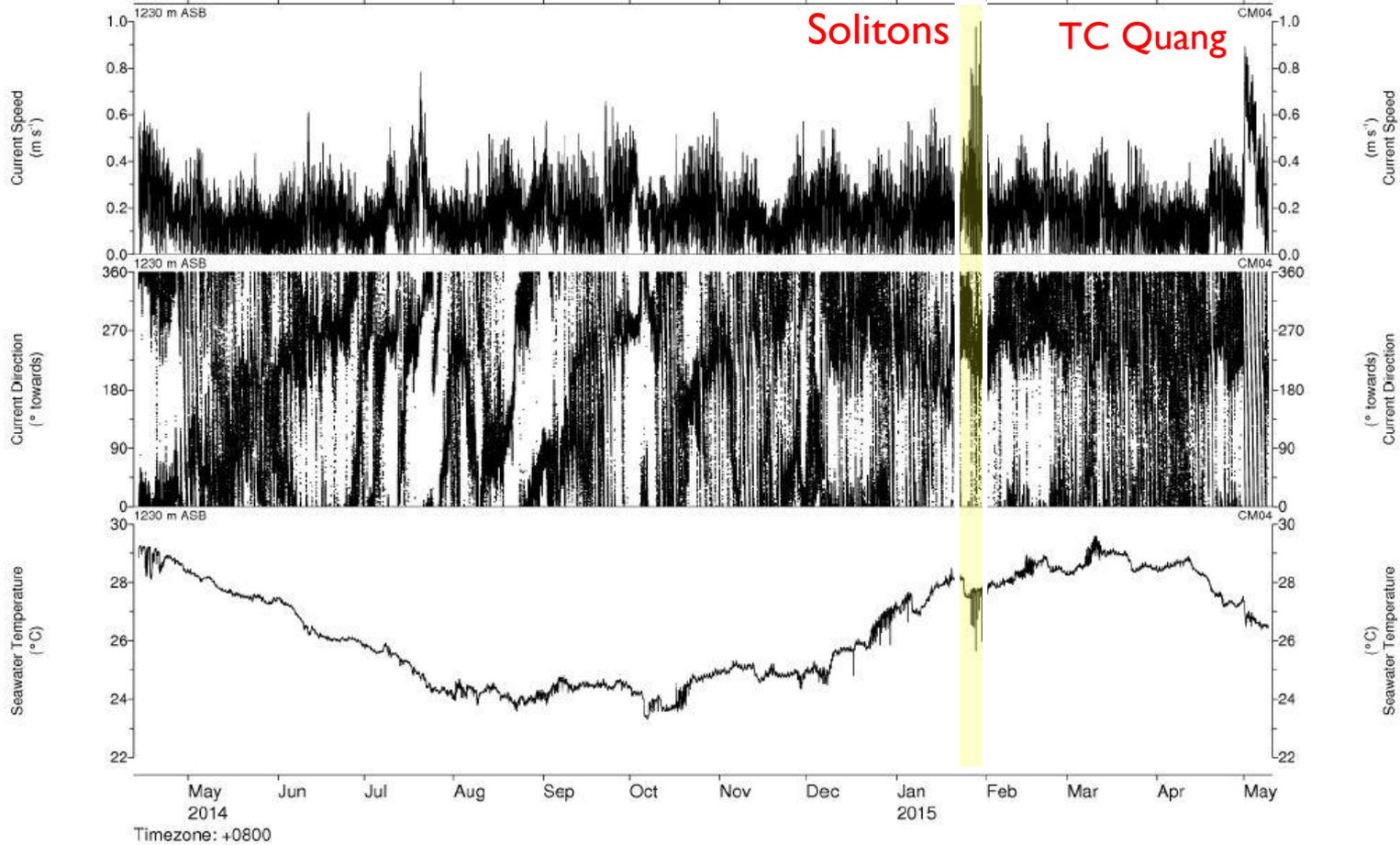
Client: Shell Development (Australia) Pty Ltd  
Project: J3003



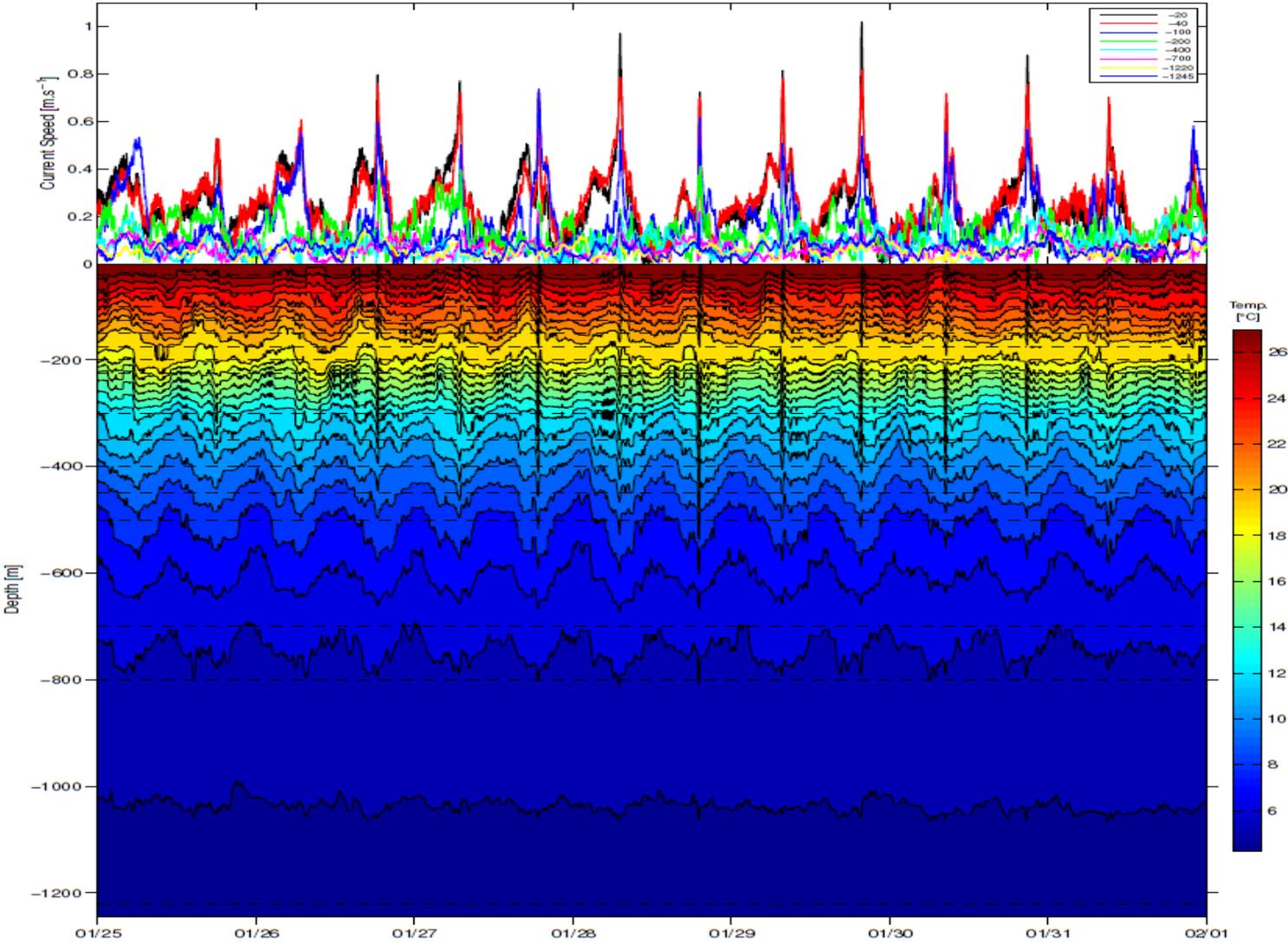


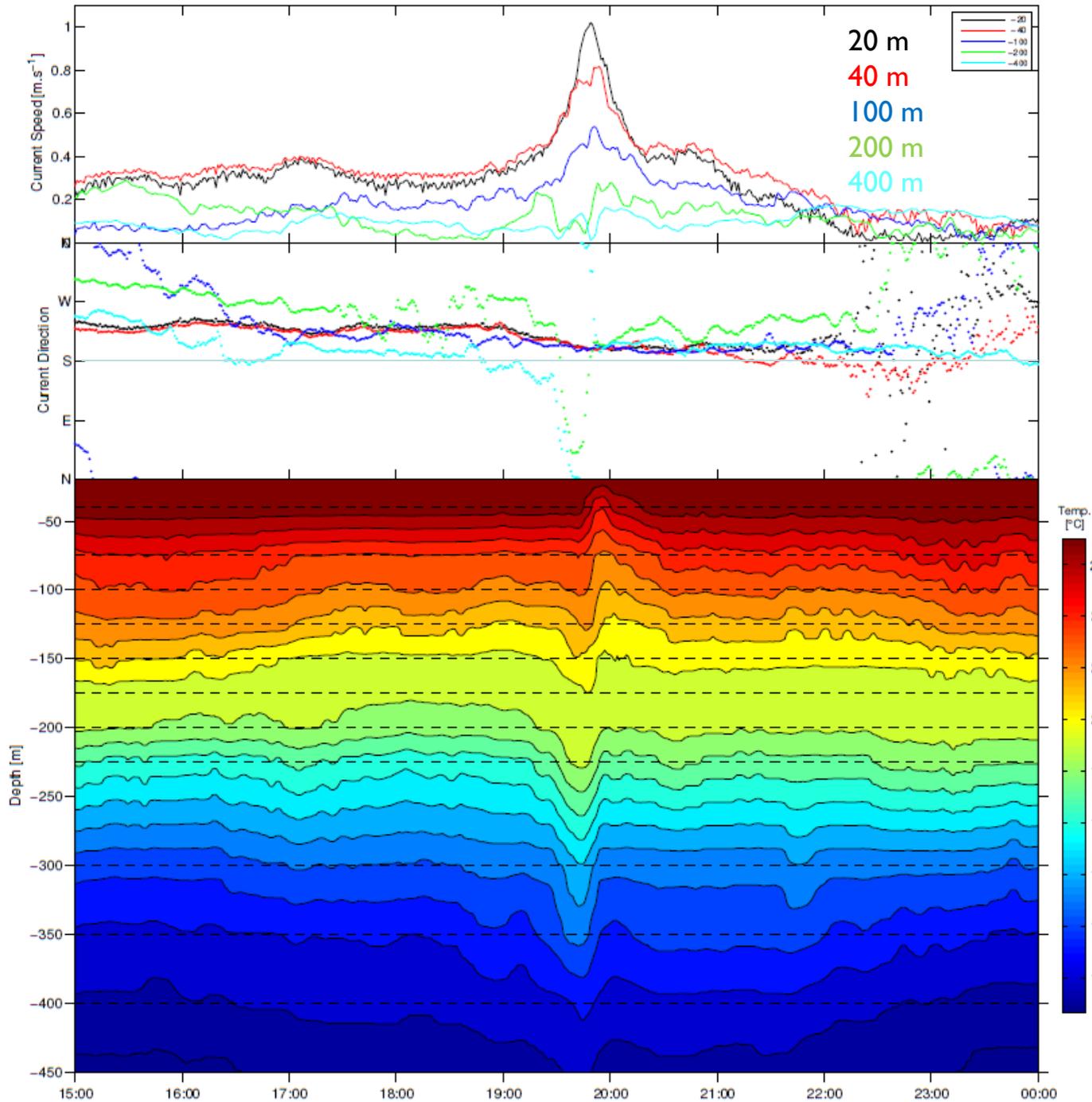
# Exmouth Surface Currents – Soliton Sequence

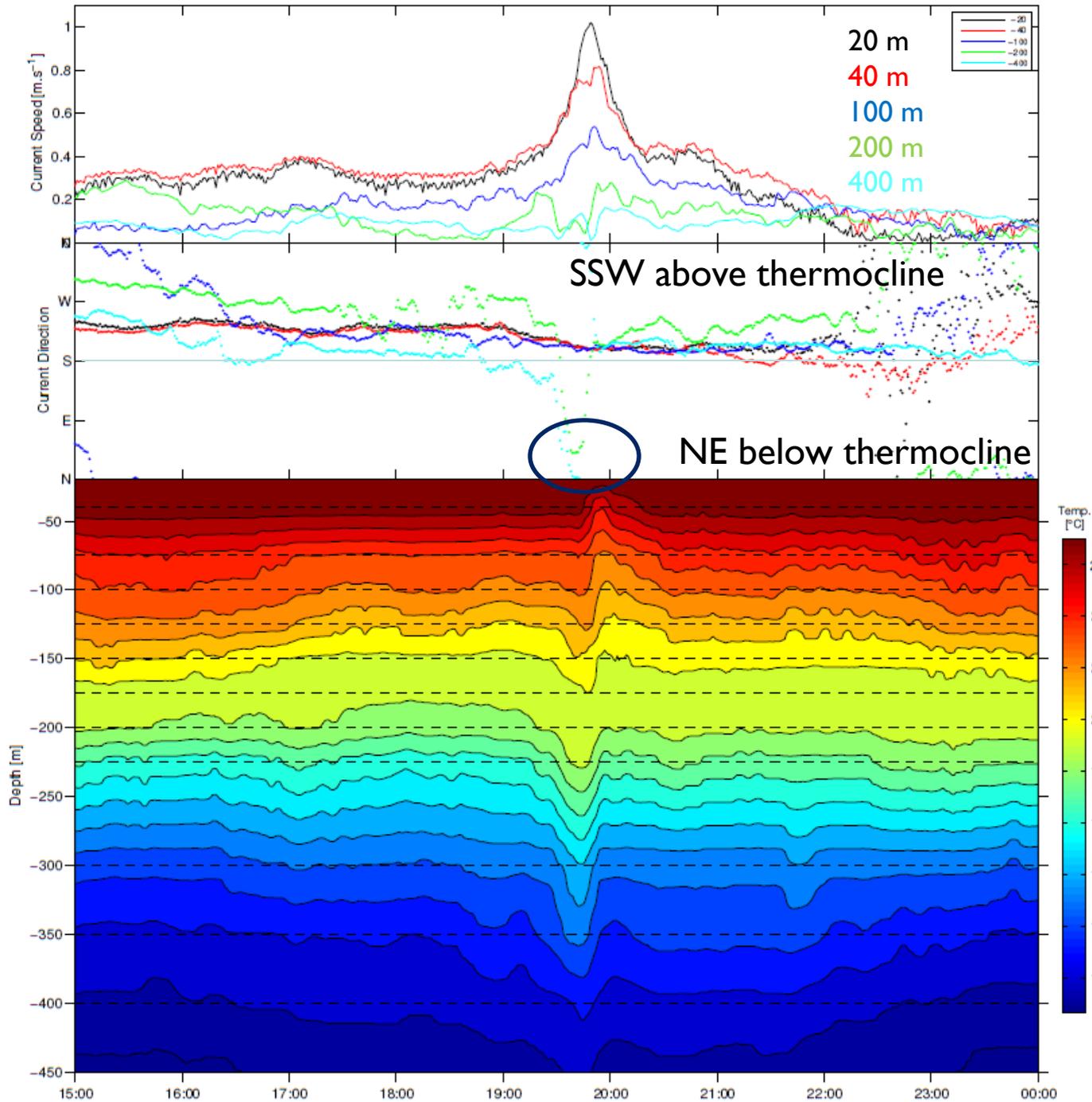
<b>Location:</b>	<b>Outer Exmouth Plateau</b>	<b>Client:</b>	Shell Development (Australia) Pty Ltd
Latitude:	19° 50' 4" S	Project:	J3003
Longitude:	112° 38' 38" E		
Location Water Depth:	1250.00 m MSL		



# The Super Soliton Series

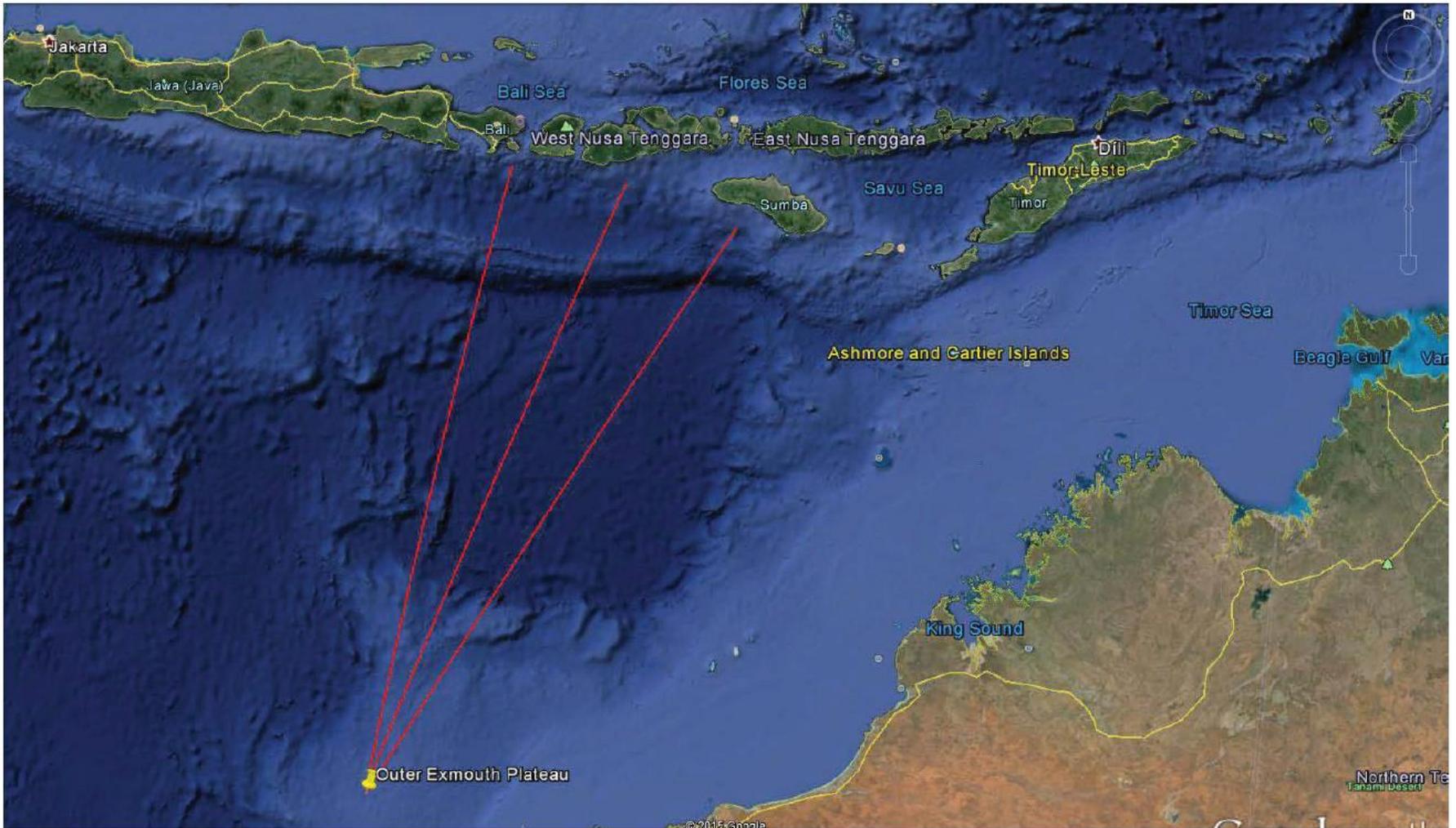






# Their Likely Source

- Thermal structure shows they are Vertical Mode I (VMI).
- Peak speeds in upper layer in the direction of propagation.
- Back-track along Great Circle Route.
- Lombok and Sape Straits (both known internal wave generation locations) bound the potential generation arc.
- Argo Data provides 'typical' density structure.
- Simple KdV calculations suggest a propagation speed of  $2.5 \text{ m s}^{-1}$ .
- Propagation time  $\sim 6$  days.



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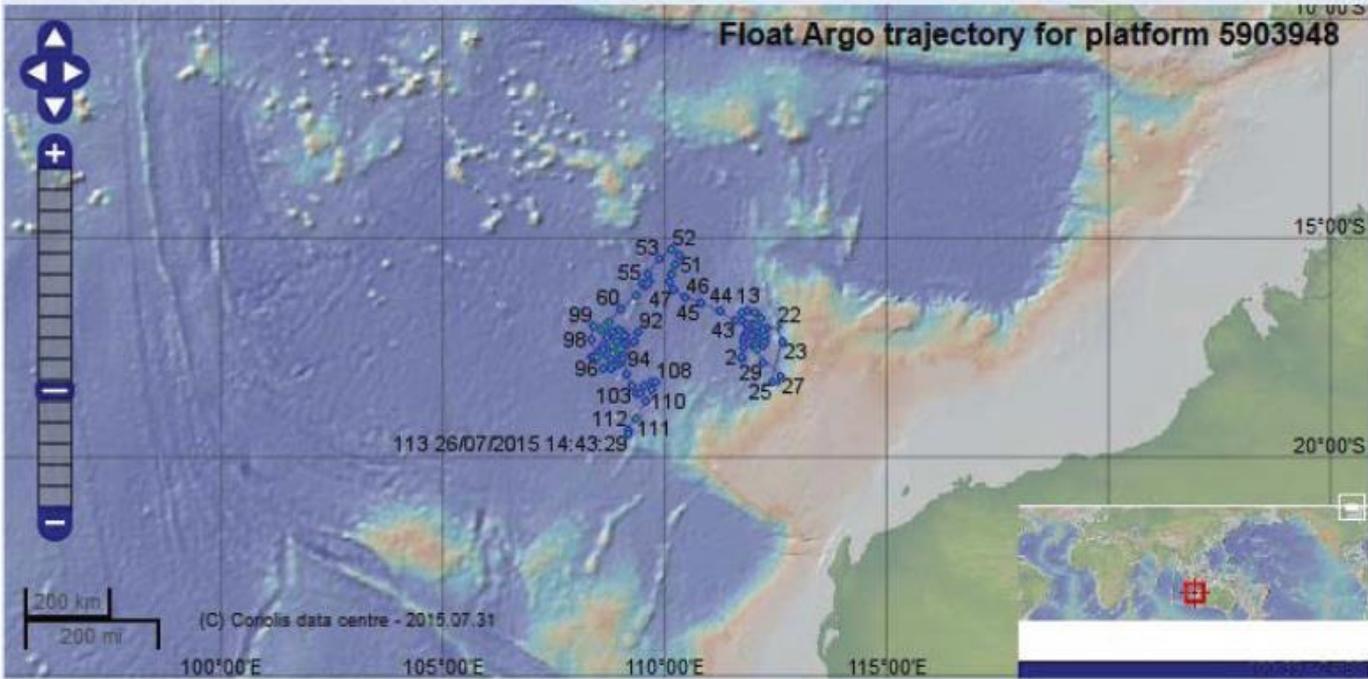
## Lombok Strait

- Known area of internal wave generation.
- Shallow sills (~ 200 m)
- Strong Tidal currents in between Islands

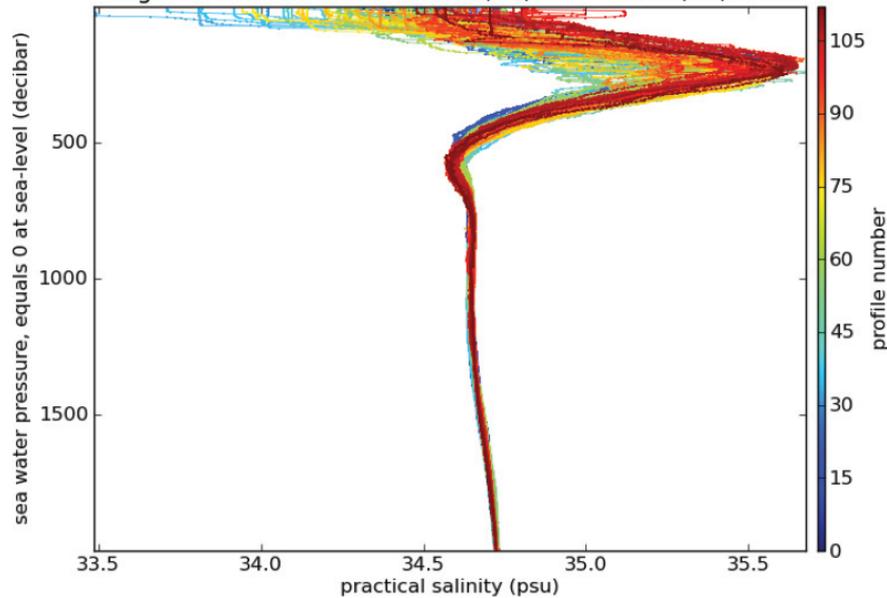
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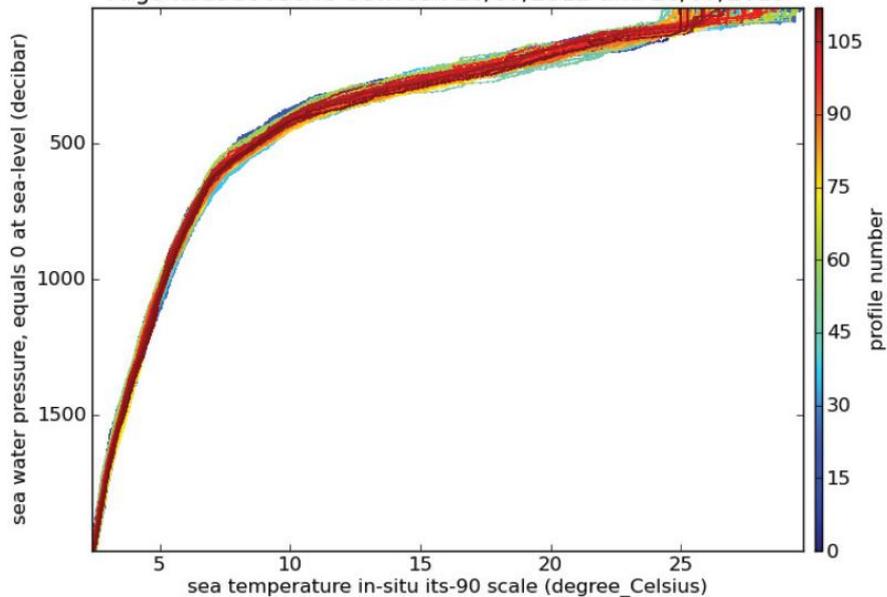
# Argo Float Trajectory from 26/4/12 – 26/07/15



Argo float 5903948 between 26/07/2012 and 26/07/2015



Argo float 5903948 between 26/07/2012 and 26/07/2015



Lombok Strait to Outer Exmouth - rough KdV Calcs

Trial		1	2	3
Nominal Depth (m)		1250	1500	2000
u1	m s <sup>-1</sup>	1	1	1
Bearing	°	205	205	205
h1	m	150	150	150
h2	m	1100	1350	1850
rho1	kg m <sup>-3</sup>	1025	1025	1025
rho2	kg m <sup>-3</sup>	1030	1030	1030
C	m s <sup>-1</sup>	2.51	2.54	2.57
C0	m s <sup>-1</sup>	2.51	2.54	2.57
eta	m	69.47	67.50	65.29
u2	m s <sup>-1</sup>	0.16	0.13	0.09
Propagation Distance	km	1300	1300	1300
Propagation Time	days	6.0	5.9	5.9

Phase Speed ~ 2.5 m s<sup>-1</sup>

Propagation Time ~ 6 days

Upper Level Speed ~ 1 m s<sup>-1</sup>

Lower Level Speed ~ 0.15 m s<sup>-1</sup>

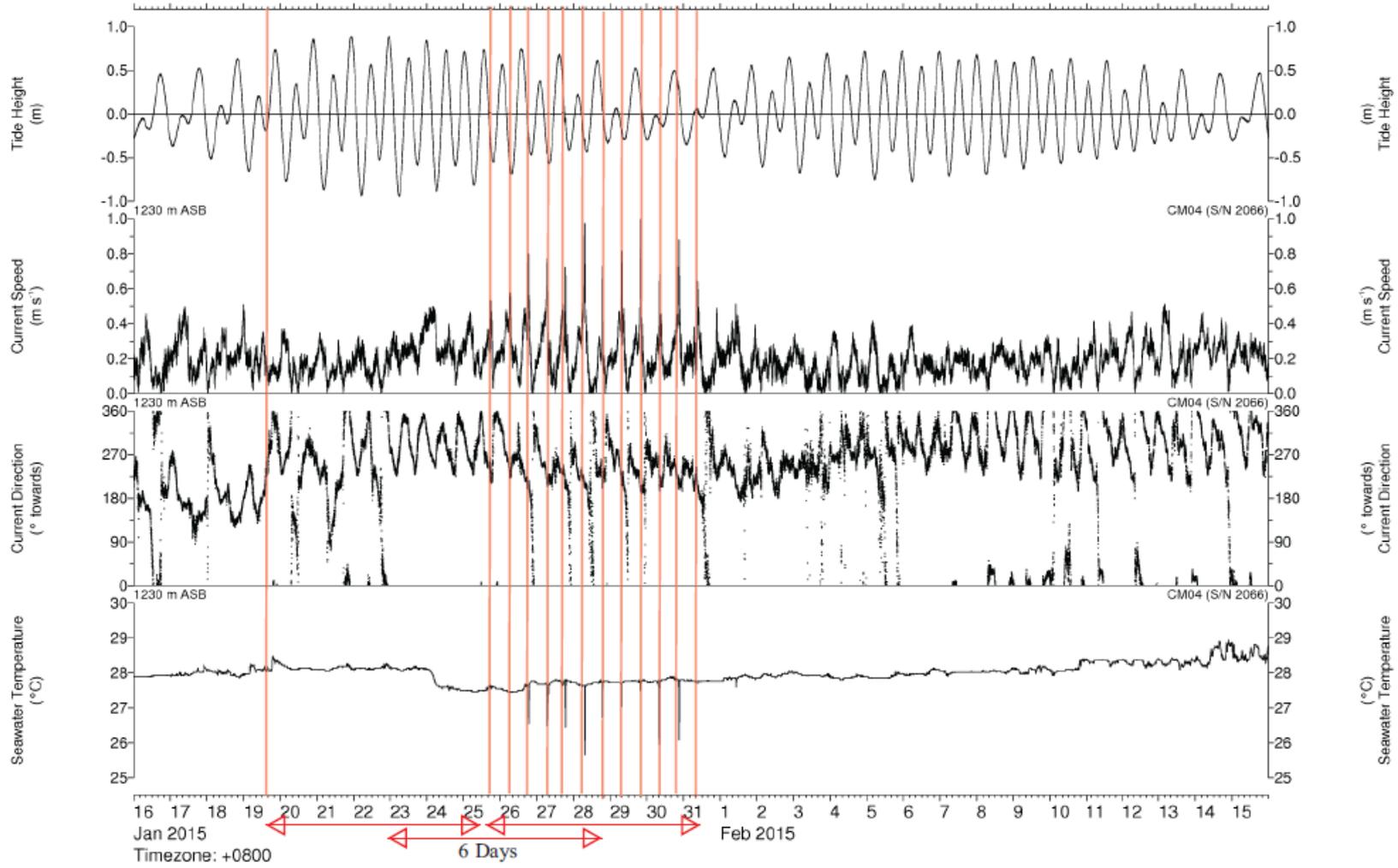
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**Location: Outer Exmouth Plateau**

Latitude: 19° 50' 4" S  
Longitude: 112° 38' 38" E  
Location Water Depth: 1250.00 m MSL

Client: Shell Development (Australia) Pty Ltd  
Project: J3003



Time Zone: UTC +08:00 hours      Data Source: /data/jobs/J3003/measured/CM04/oct14/3003out\*\_current.c.nc  
© RPS MetOcean Pty Ltd      moetimehist: 11:58 4/Aug/2015 by dennis.foo (timehist.OuterExmouthPlateau.currents.1230mASB.Fig12.28.ps)

# The Upshot

Long-travelled solitons have the potential to generate higher riser loadings than tropical cyclones in deep waters off Australia's North West Shelf

We believe that we need to include **Indonesian Straits** in any comprehensive soliton modelling for the North West Shelf

We can establish this via running of the “adjoint” of a hydrodynamic model (we chose MITgcm).

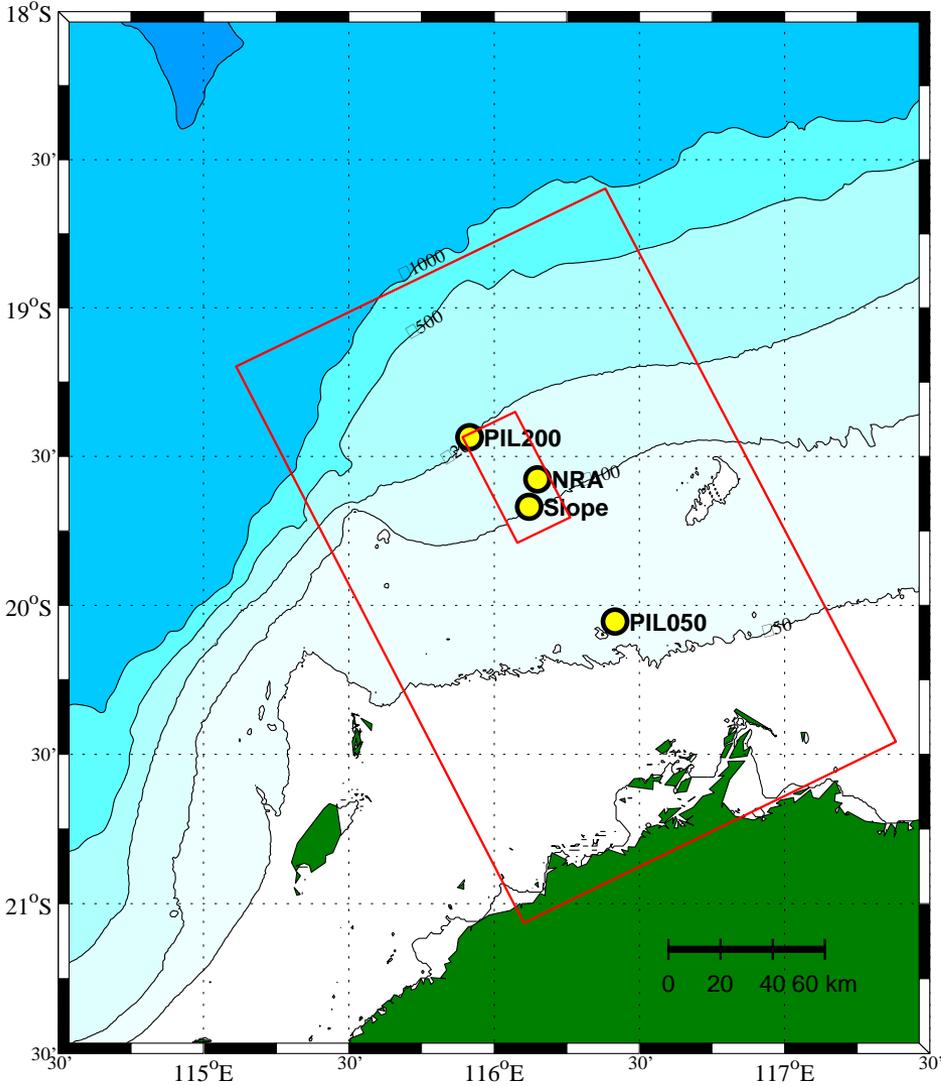
We focused on data from IMOS PIL200 location, because these data are publicly available.

# Locations of Measured Data

**PIL200, PIL100 and PIL50** – IMOS data in 200, 100 and 50 m depth, respectively

**NRA** – RPS data in 125 m depth

**Slope, Break and Shelf** – ARC data in 100, 80 and 78 m depth, respectively.



# Adjoint MITgcm Modelling

The Adjoint of MITgcm calculates the **sensitivity** of a **cost function** to **model state variables** and input data.

**Model State Variables** and input data include

- tidal forcing
- density structure
- bathymetry (seabed slope)

The **Cost Function** is defined as

- the (VMI) isopycnal displacement at PIL200 location

**Sensitivity** can be expressed wrt vertical modes, the theory of which relates 'forcing' (of VMI) from the barotropic tide (VM0).

# The Adjoint of the MITgcm Model

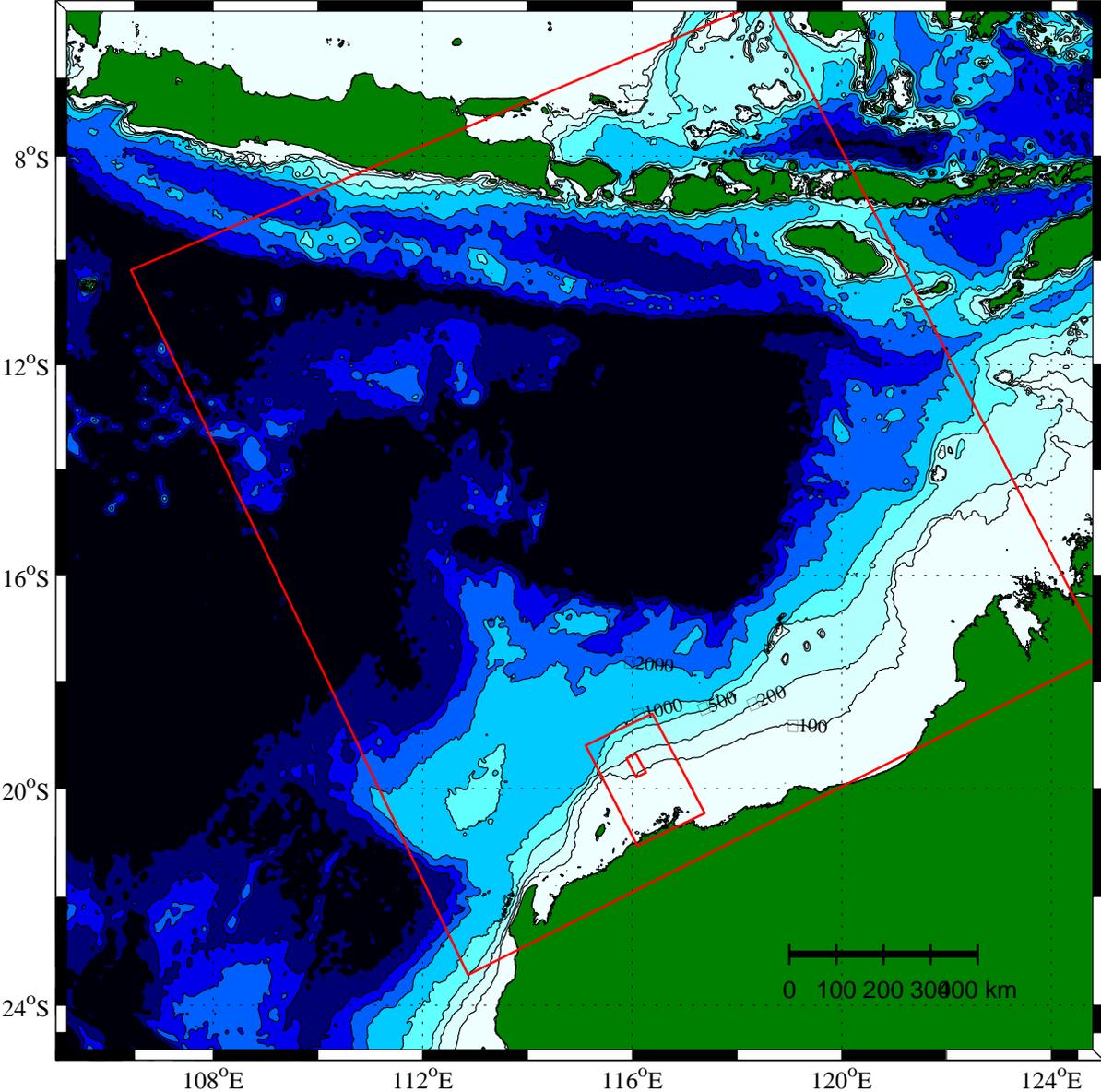
Is **used to assess the sources** of energy affecting internal wave motion - in this study - at PIL200 location.

The **Cost Function** (the only non-zero initial condition in the model domain) is set as **the positive VMI isopycnal displacement about PIL200 location**.

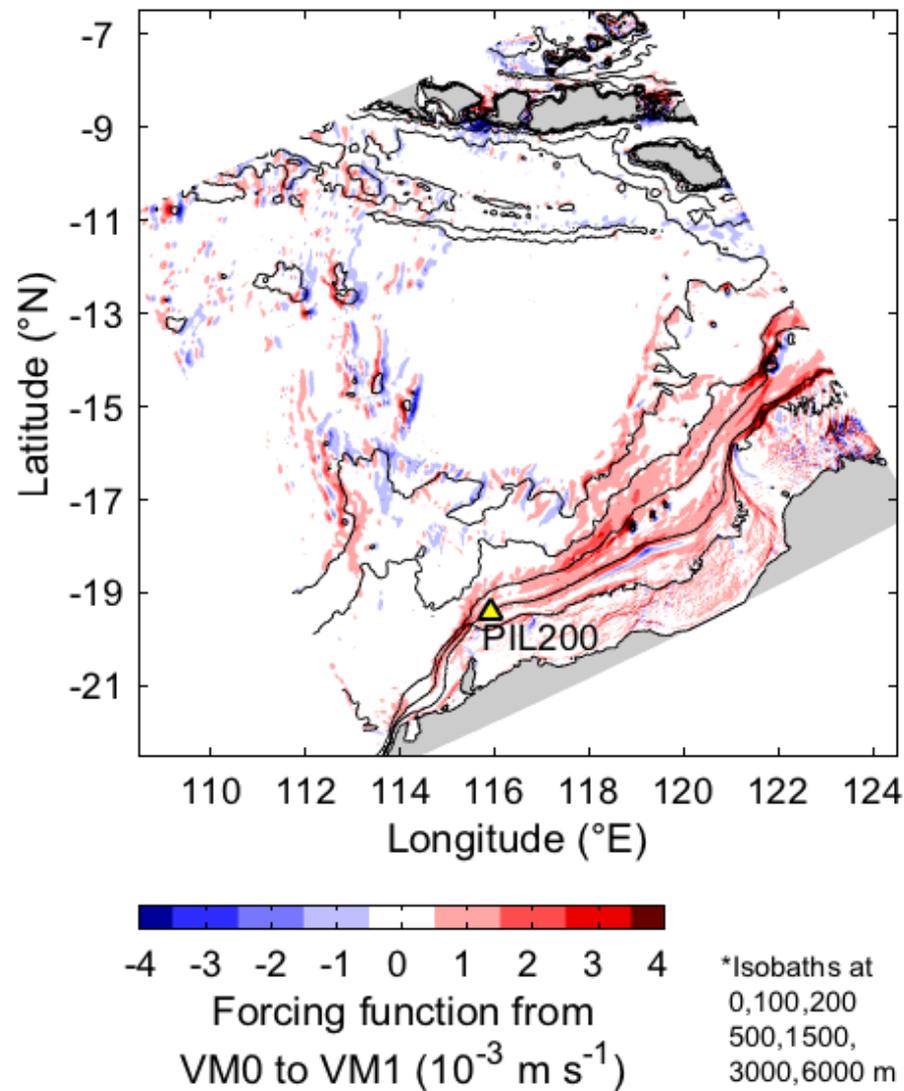
The **Forcing Function** is a direct computation of the efficiency of energy **conversion from VM0 (barotropic) to VMI (baroclinic)** motion, given bottom slope and density structure.

The **Sensitivity** of the Cost Function to remote Forcing is **calculated by stepping the model 'backwards' in time**.

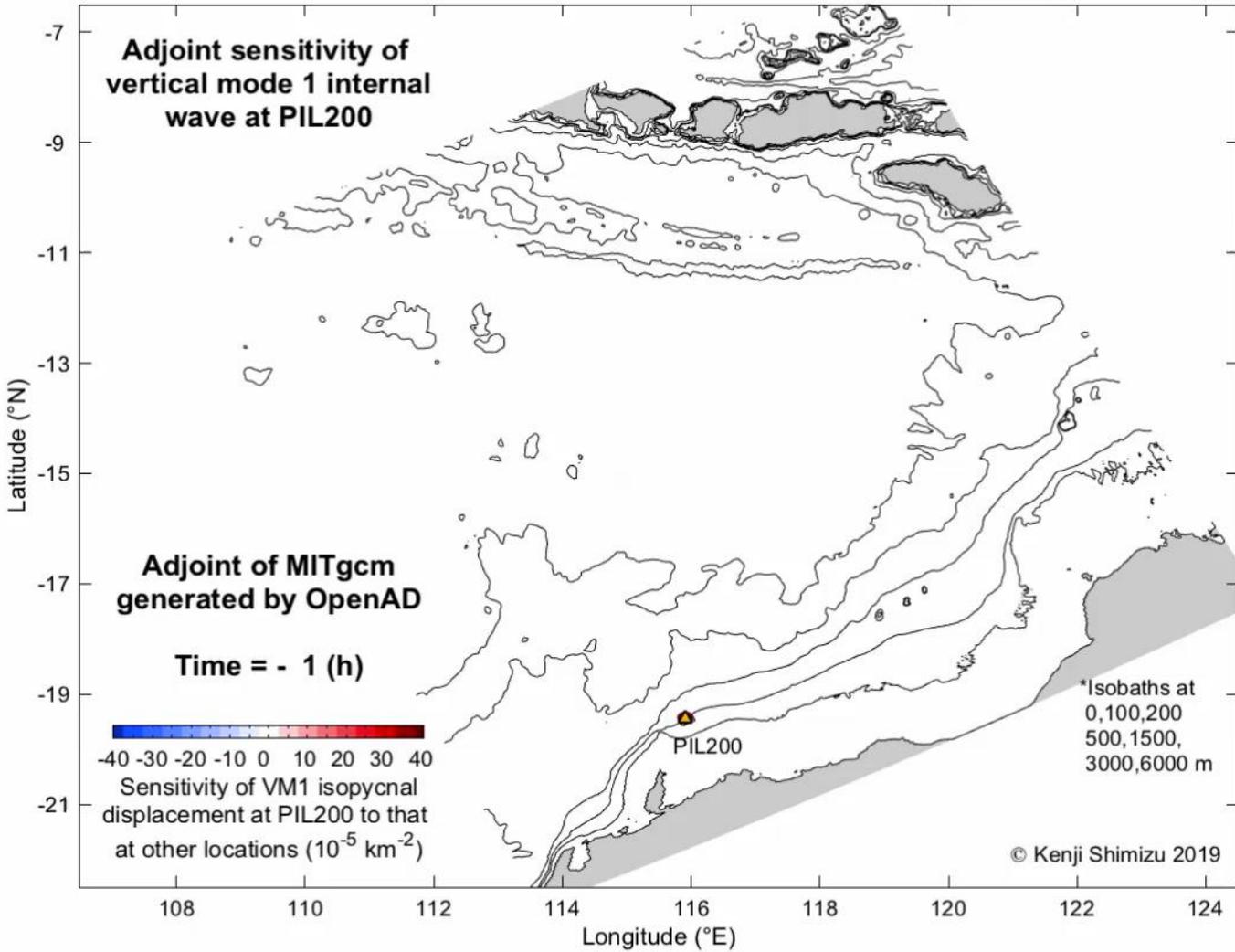
# Domain of the Adjoint Model



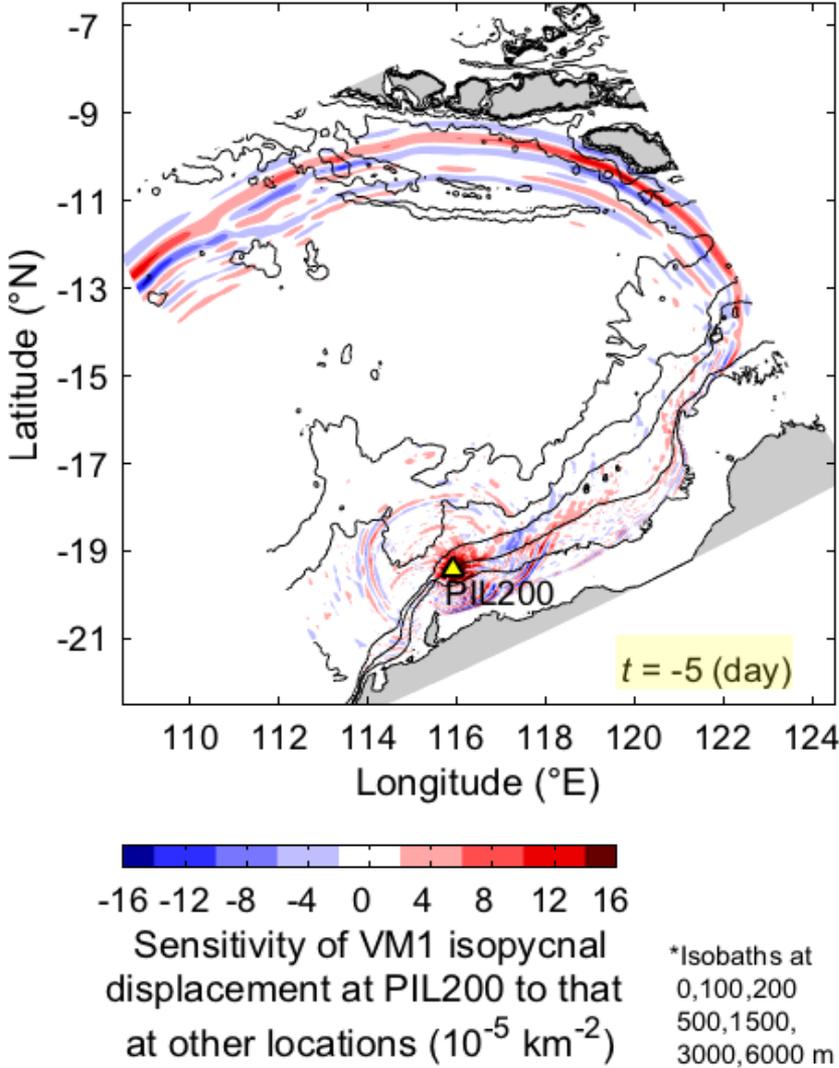
# Forcing Function for $M_2$ Internal Tide



# Sensitivity of PIL200 ISW - Animation



# Sensitivity of ISW Vertical Displacement



# Regional Contribution to ISWs at PIL200

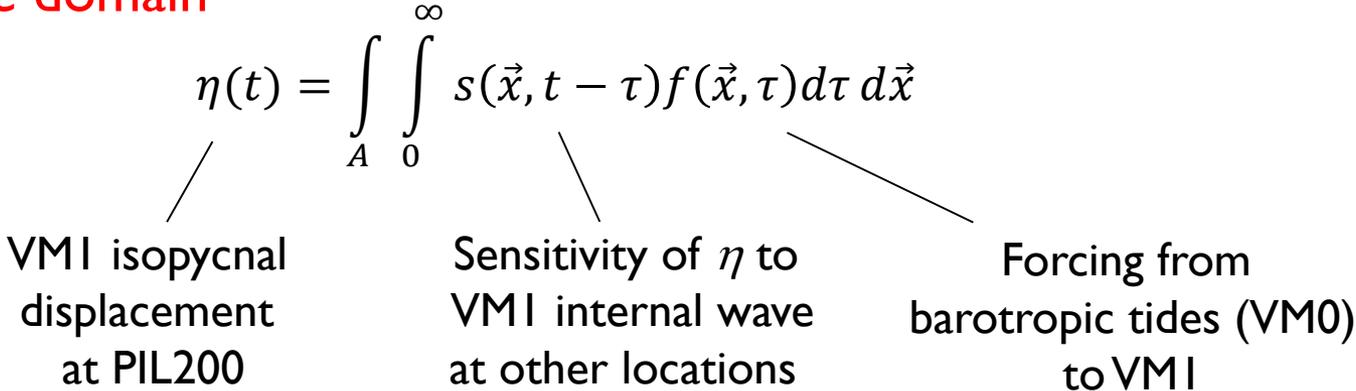
The **Source Function** describes the regional contribution to VMI  $M_2$  tide at PIL200 location.

In **time domain** (for time lag  $\tau$ ), it is the **convolution of the Sensitivity and the Forcing Function**.

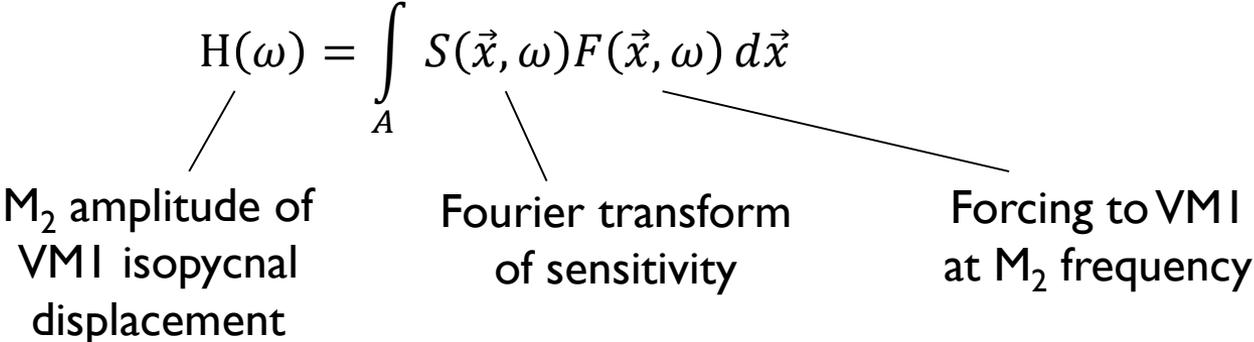
In the **frequency domain**, at a given frequency  $\omega$  (in this case the tidal  $M_2$  frequency), it is the **product of the Fourier transform of the Sensitivity and the Forcing Function**.

# Frequency Response Analysis

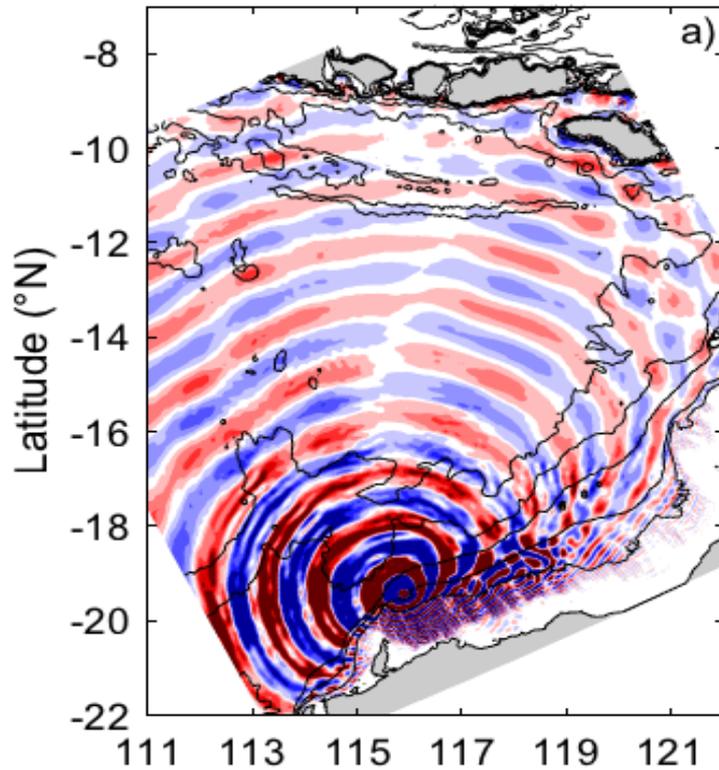
In time domain



In frequency domain (applying the convolution theorem in Fourier Theory)

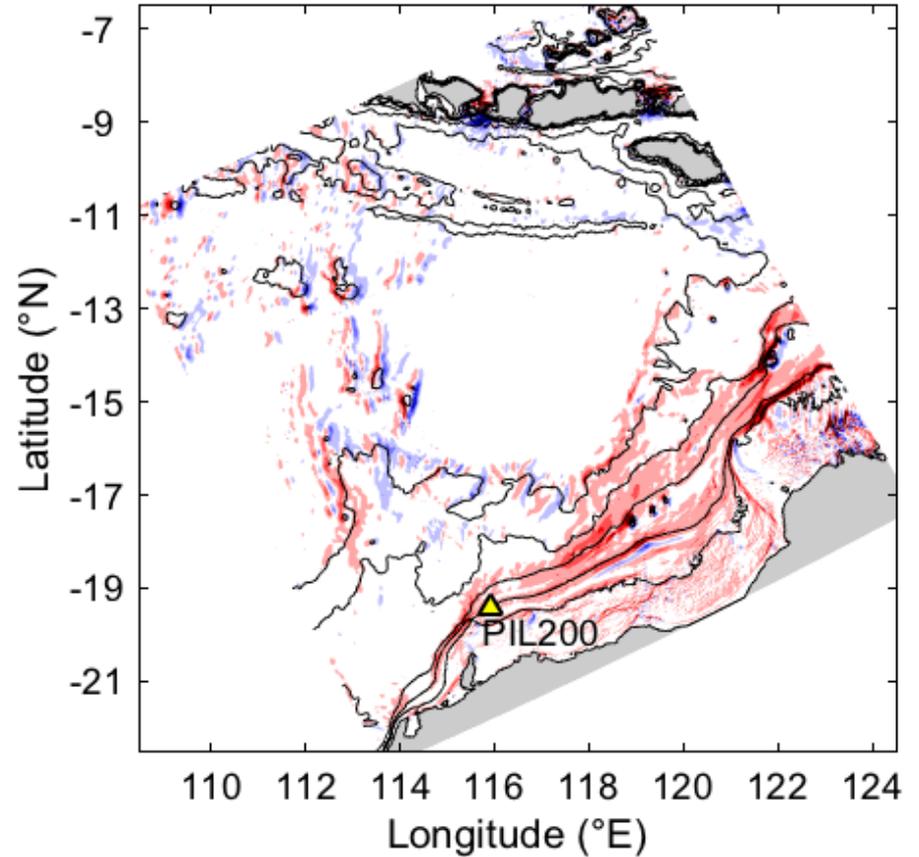


# Sensitivity x Forcing function for PIL200



Color scale: -40 -32 -24 -16 -8 0 8 16 24 32 40

Fourier-transformed sensitivity of VM1 isopycnal displacement at PIL200 to that at other locations ( $10^{-4} \text{ s km}^{-2}$ )

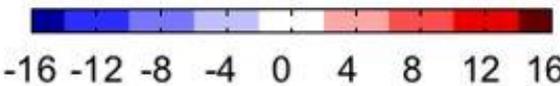
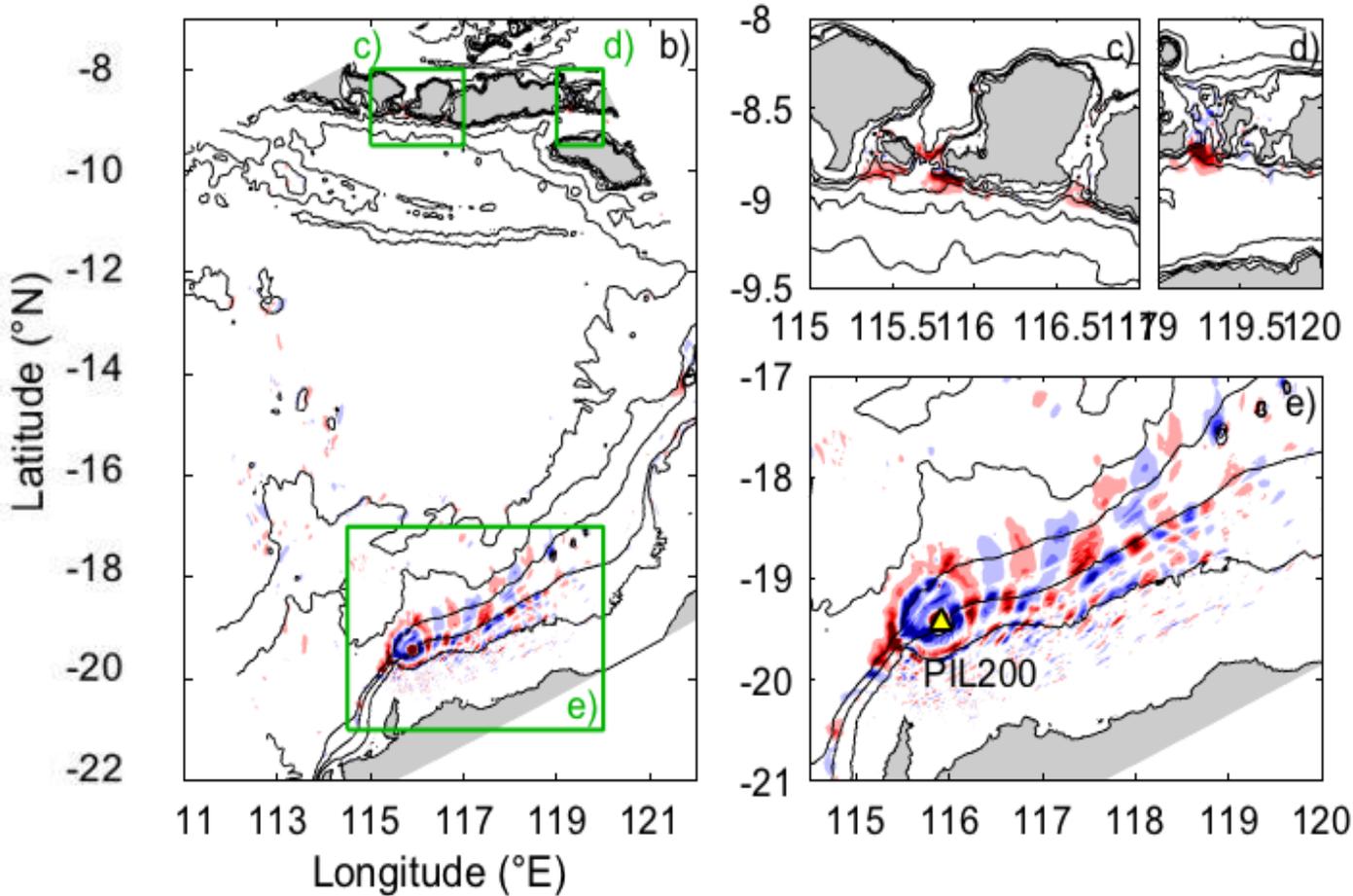


Color scale: -4 -3 -2 -1 0 1 2 3 4

Forcing function from VM0 to VM1 ( $10^{-3} \text{ m s}^{-1}$ )

\*Isobaths at 0,100,200, 500,1500, 3000,6000 m

# Source Function for ISWs at PIL200



Source function of VM1 isopycnal displacement at PIL200 ( $10^{-3} \text{ m km}^{-2}$ )

\*Isobaths at 0,100,200, 500,1500, 3000,6000 m

# Spatial Integration of the Source Function

The Source Function can be integrated over any horizontal domain to establish the relative contribution of that domain to the Cost Function (the VMI  $M_2$  tide) at PIL200 location.

Results are illustrated in the following table.



# Sources of $M_2$ Internal Tide at PIL200

VM1 M2 tide at PIL200

Region	Contribution (m)
<b>Australian North West Shelf (&lt;1500 m deep)</b>	
Lower North West Shelf (west of ~120 °E)	-6 + 18 i
Upper North West Shelf (east of ~120 °E)	-1 - 1 i
Subtotal	-7 + 17 i
<b>Indonesian region (&lt;1500 m deep)</b>	
Lombok & Bali Straits	7 + 3 i
Sape Strait	3 + 2 i
Alas Strait	1 - 0 i
Other	0 - 0 i
Subtotal	11 + 5 i
<b>Deep open ocean (&gt;1500 m deep)</b>	<b>-2 - 2 i</b>
<b>Total</b>	<b>2 + 20 i</b>

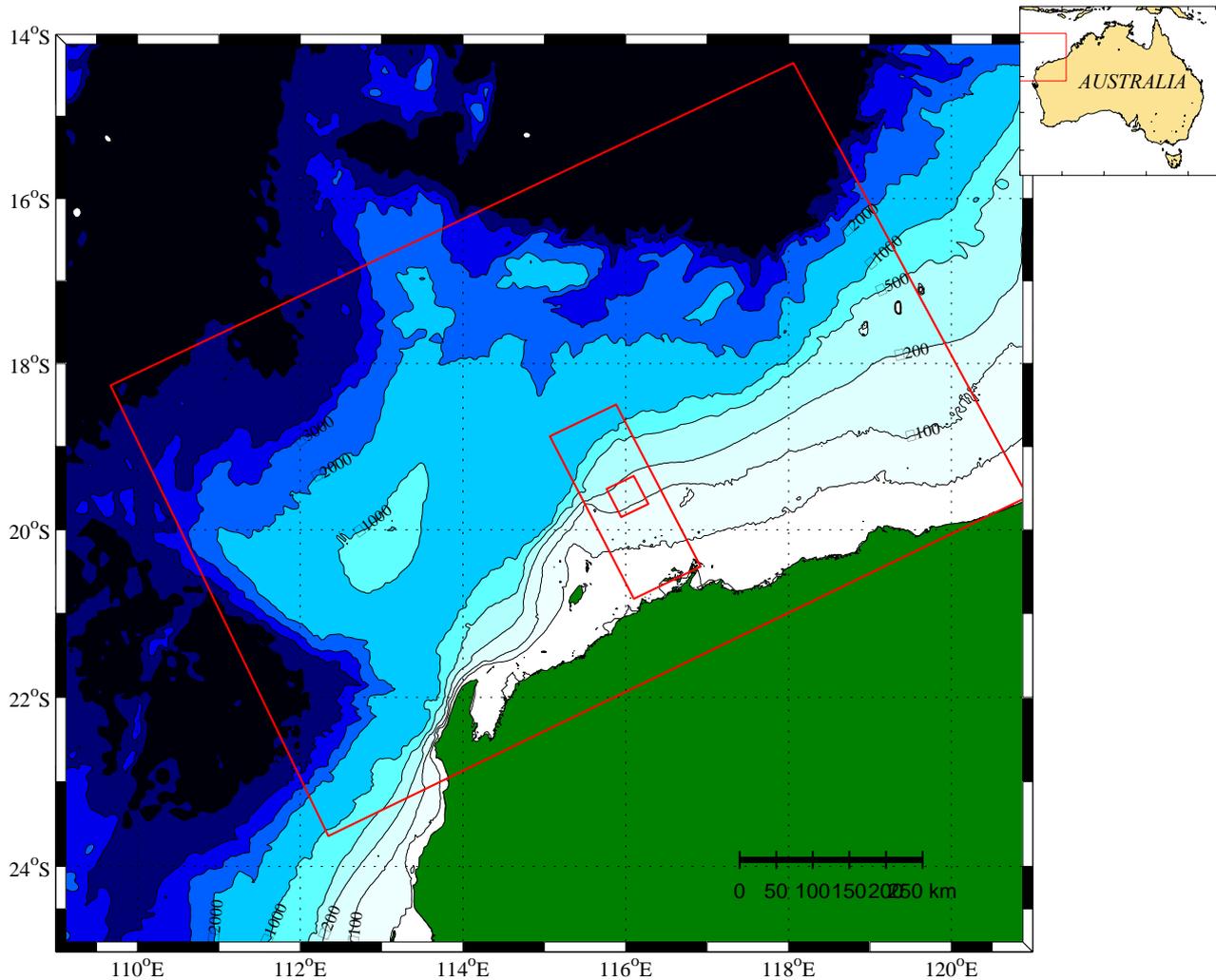
# Results of Adjoint MITgcm Modelling

We have established that the Indonesian Straits are a significant source of internal tidal energy propagating to Australia's North West Shelf.

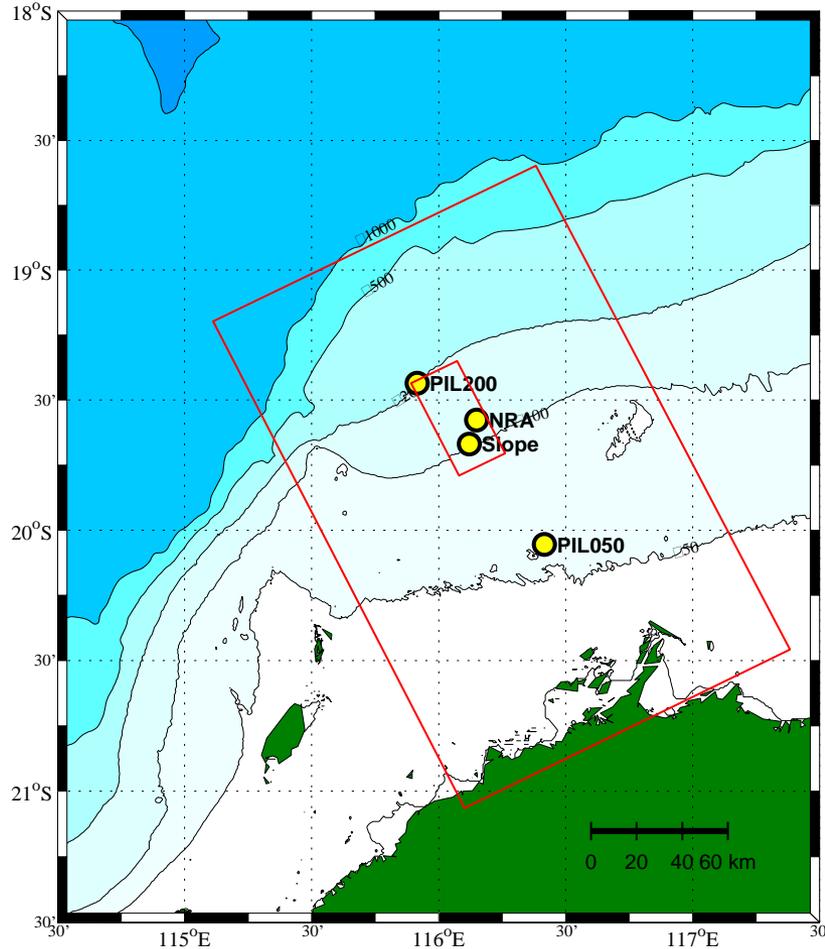
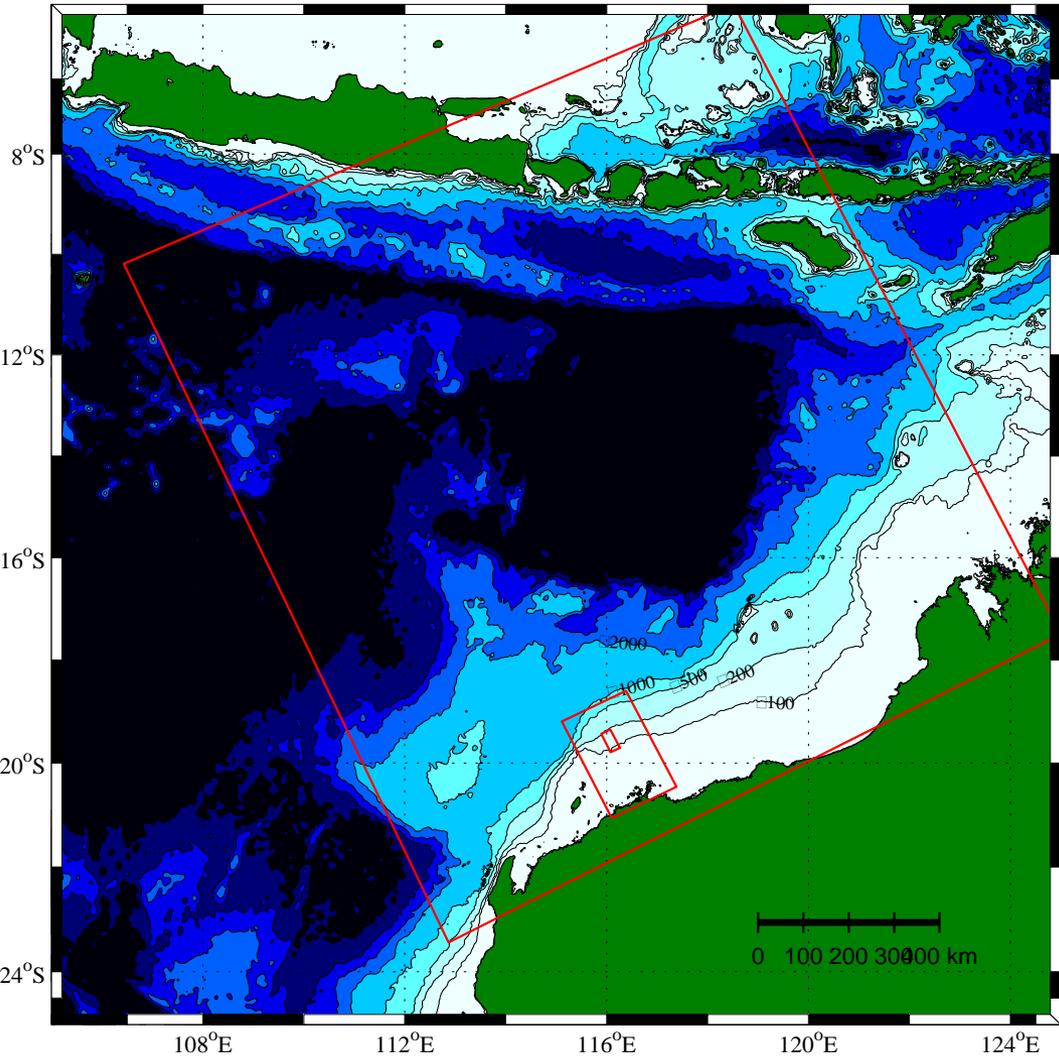
Any modelling of Internal Solitary Waves on the North West Shelf will require inclusion of these source regions in the model domain.

RPS

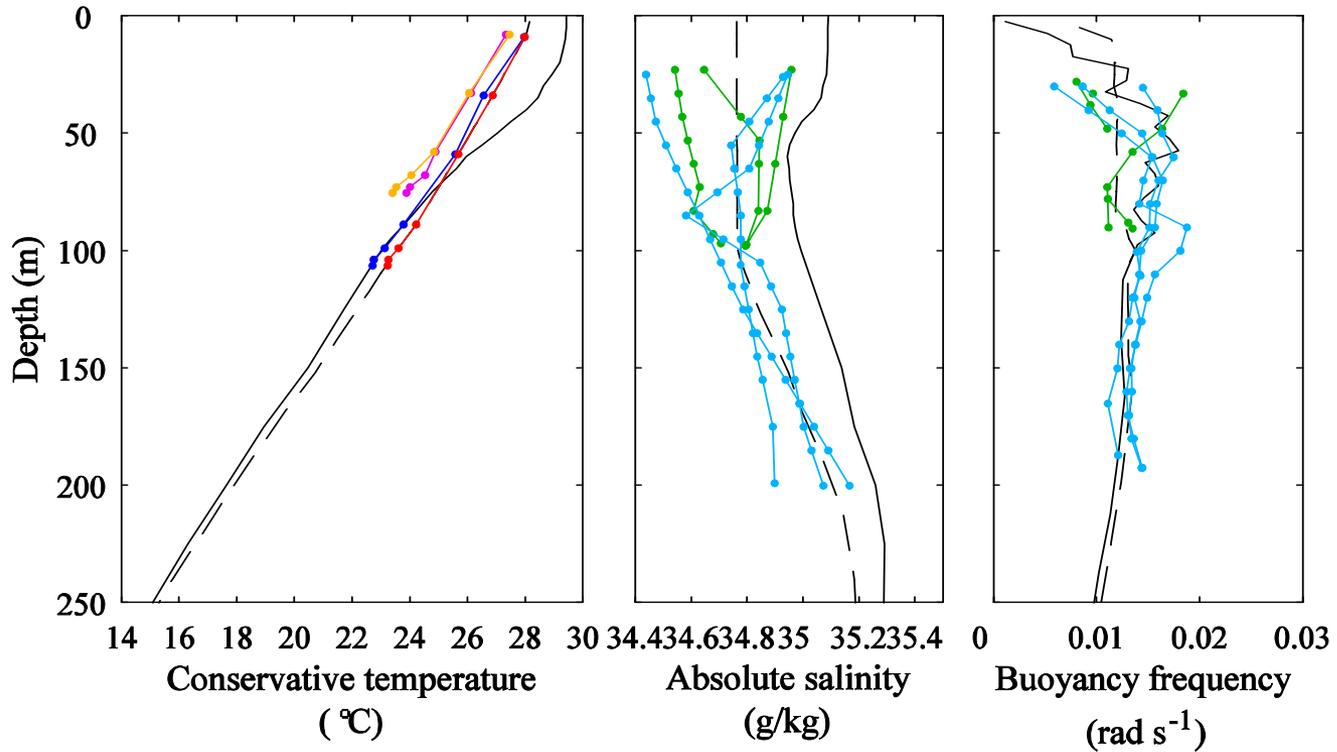
# Original (2015) Model Grid



# Revised Model Grid



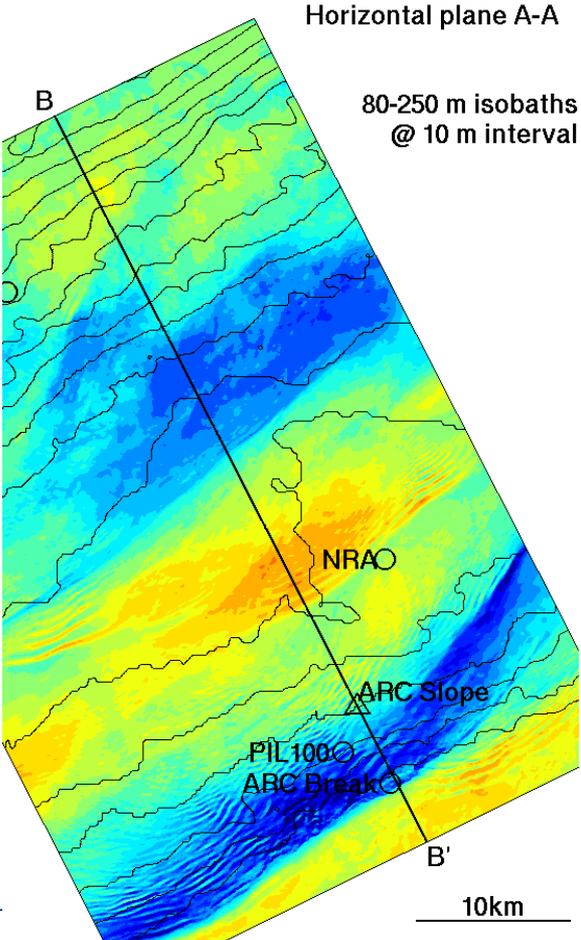
# Stratification



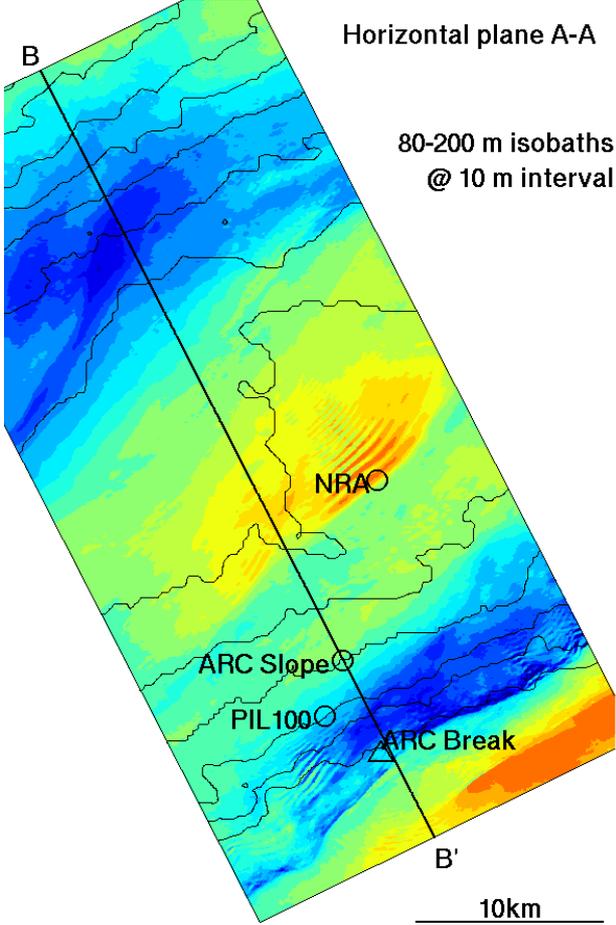
- ARC Slope (1992/Mar/29-Apr/12)
- ARC Shelf (1992/Mar/29-Apr/12)
- IMOS PIL200 (Mar 2012,2013,2014)
- WOA13 (Mar-Apr)
- ARC Break (1992/Mar/29-Apr/12)
- ARC Slope (1992/Mar/22-Apr/05)
- IMOS PIL100 (Mar 2012,2013,2014)
- Initial condition (baseline)

# Comparison of Configurations

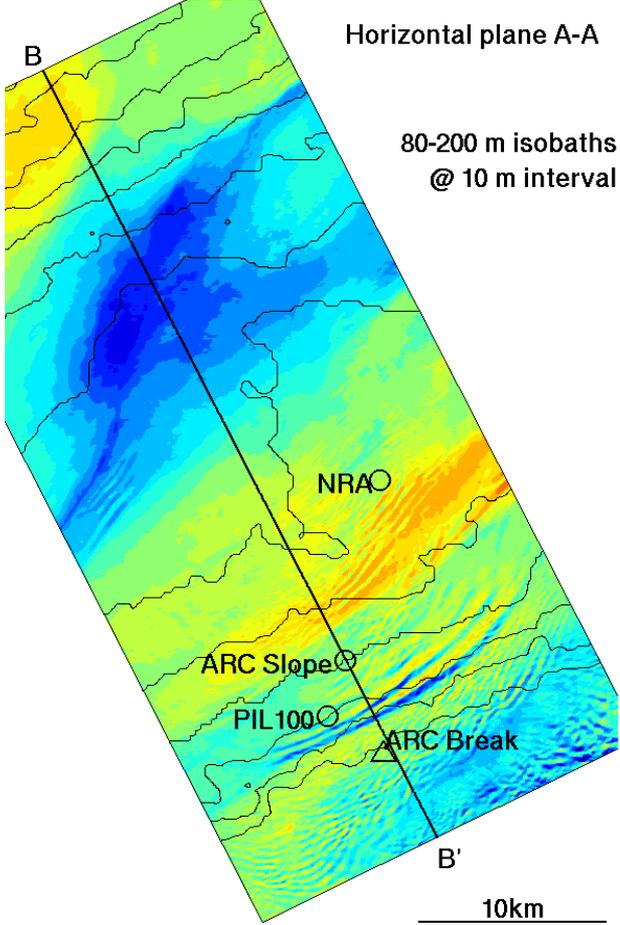
## Initial grid



## Revised grid Initial T/S

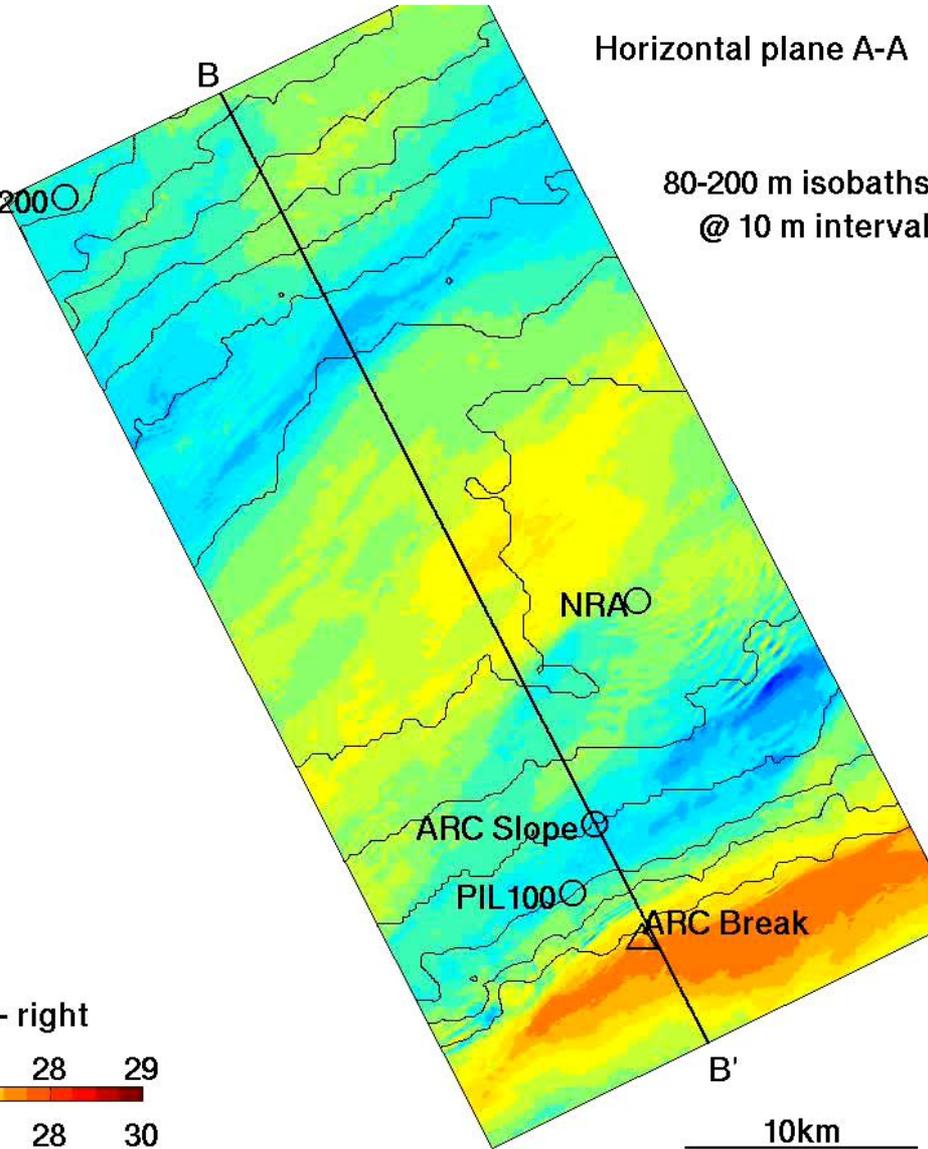
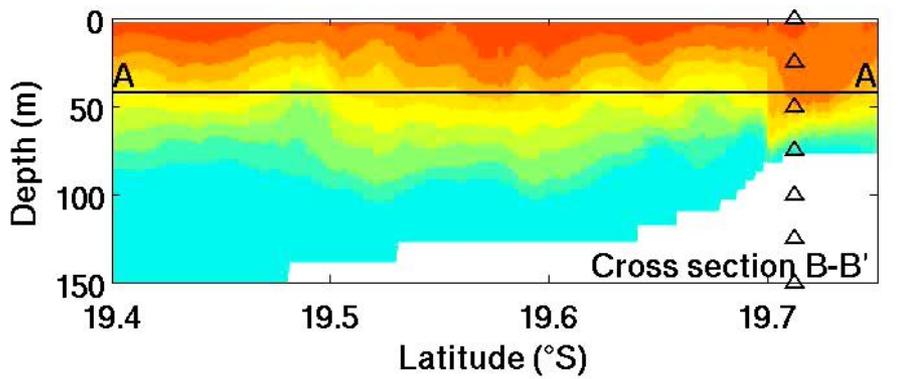
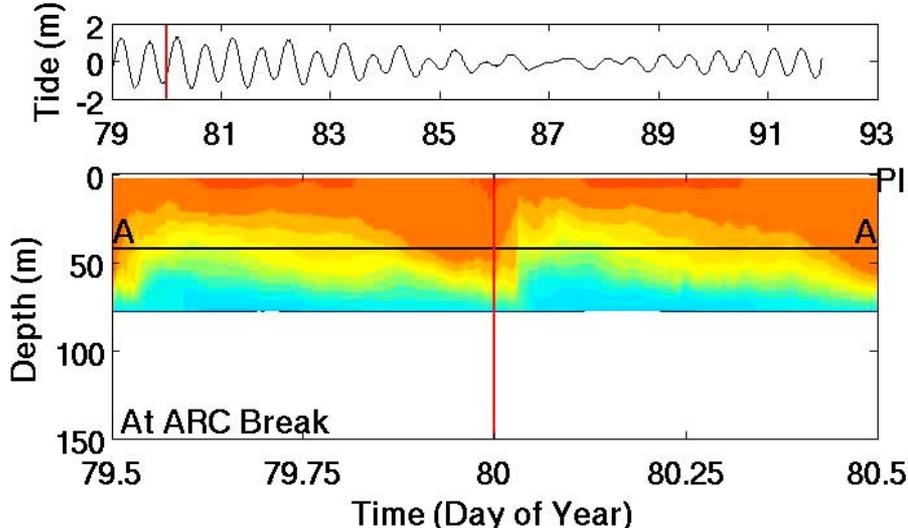


## Revised grid Revised T/S

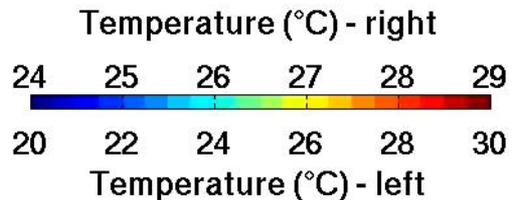


RPS

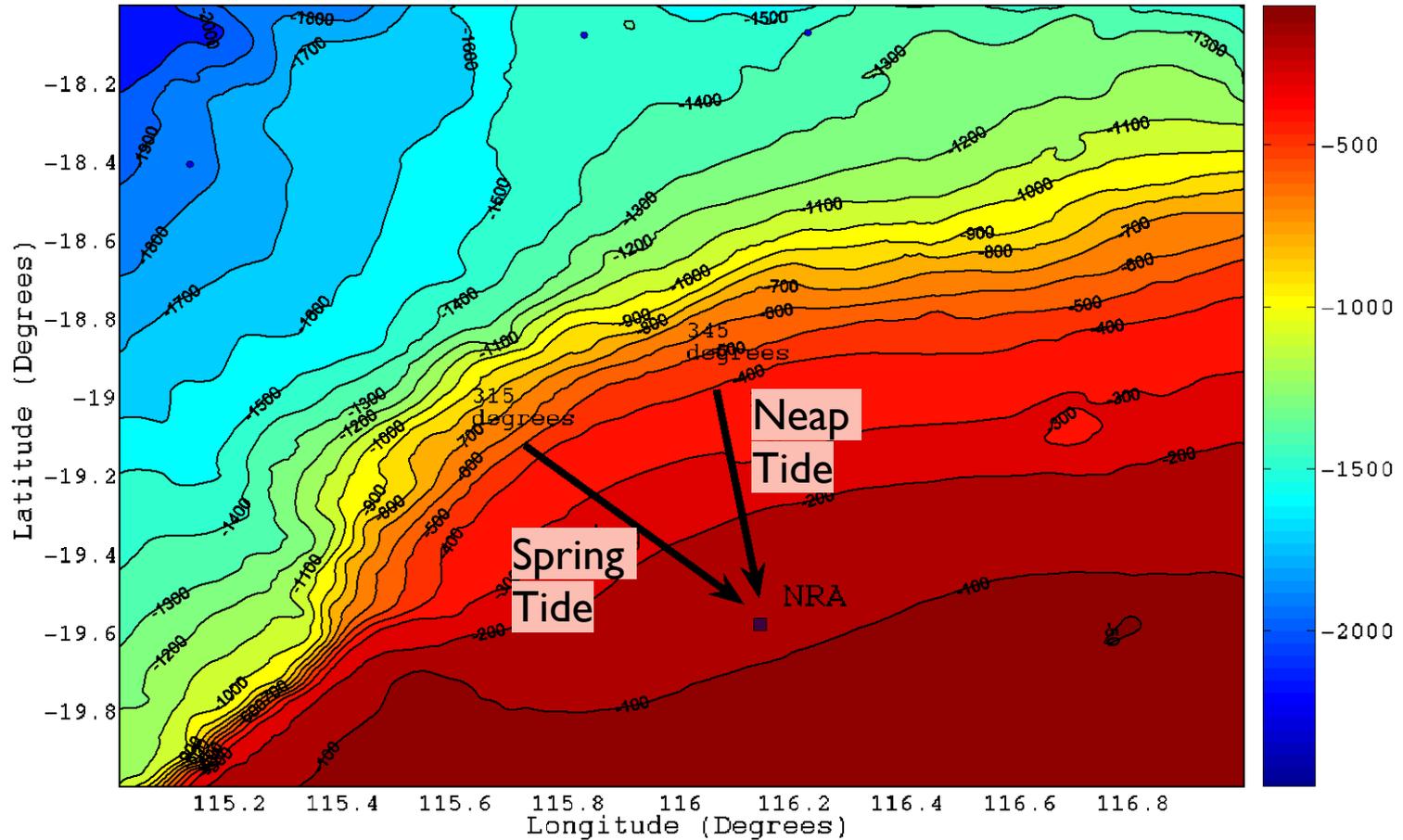
# ARC Measurements – Model Animation



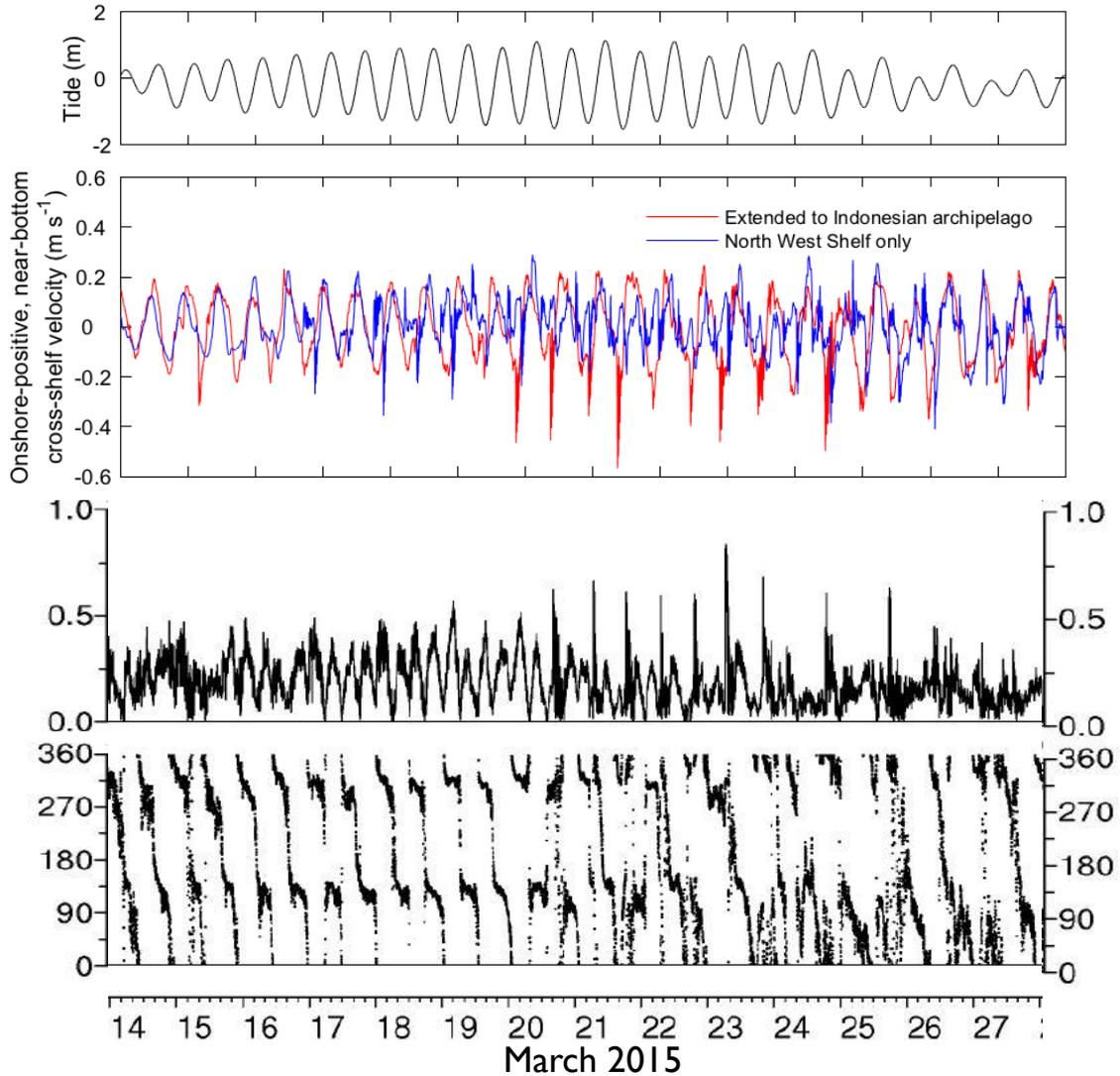
MITgcm  
North Rankin region  
1992-03-21 00:00:00



# NRA Solitons - van Gastel et al. 2009



# (Rough) Comparison with Measurements

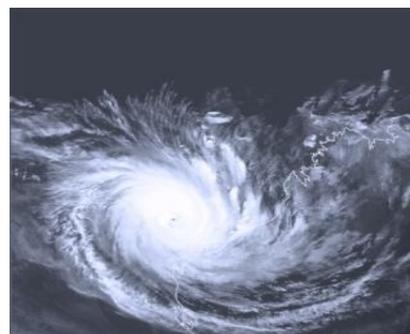


# What we have learned

1. Established that **Indonesian Straits** are important source regions of internal waves affecting Australia's North West Shelf
2. ISWs are highly **sensitive to stratification**.  
Stratification is very difficult to model (without drift)
3. Solitons lose lateral coherence as they propagate inshore
4. MITgcm requires further enhancement before it can reliably hindcast Internal Solitary Waves



# Thank you



For further information:  
[stevejbuchan@hotmail.com](mailto:stevejbuchan@hotmail.com)  
[kenji.shimizu.rc@gmail.com](mailto:kenji.shimizu.rc@gmail.com)